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# Measurement of the neutral current cross section and $F_2$ structure function for deep inelastic $e^+p$ scattering at HERA

ZEUS Collaboration

## Abstract

The cross section and the proton structure function  $F_2$  for neutral current deep inelastic  $e^+p$  scattering have been measured with the ZEUS detector at HERA using an integrated luminosity of  $30 \text{ pb}^{-1}$ . The data were collected in 1996 and 1997 at a centre-of-mass energy of 300 GeV. They cover the kinematic range  $2.7 < Q^2 < 30000 \text{ GeV}^2$  and  $6 \cdot 10^{-5} < x < 0.65$ . The variation of  $F_2$  with  $x$  and  $Q^2$  is well described by next-to-leading-order perturbative QCD as implemented in the DGLAP evolution equations.

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# 1 Introduction

The measurements of the differential cross-section and  $F_2$  structure function in neutral current (NC) deep inelastic scattering (DIS) at HERA have been vital in testing the predictions of perturbative QCD and in the determination of the parton densities in the proton at low  $x$ . In both of these areas of study the accuracy and precision of the measurements are of paramount importance.

The measurements of the double-differential cross-section  $d\sigma^{ep}/dx dQ^2$  and  $F_2^{em}$  presented here are based on an  $e^+p$  DIS event sample twelve times larger than that used in the previous ZEUS publication [1]. This increase, combined with an improved understanding of the detector, results in a significant decrease in both the statistical and systematic uncertainties<sup>1</sup>. The uncertainties are systematics dominated for  $Q^2 < 800 \text{ GeV}^2$ .

The outline of the paper is as follows: in Section 2, the kinematics and the cross section of  $e^+p$  NC DIS are discussed; in Sections 3 and 4, the experimental conditions and the trigger used in the data taking are presented; Section 5 explains the method of the reconstruction of the kinematic variables; in Section 6, Monte Carlo simulations used in the analyses are described; Sections 7 and 8 discuss the details of the basic measured quantities; in Section 9, the characteristics of the selected events are examined; Section 10 presents the results; and Section 11 contains the conclusions.

## 2 Kinematics and cross section

The kinematics of the deep inelastic scattering process,  $e(k) + p(P) \rightarrow e(k') + X$ , can be completely described by the negative of the four-momentum transfer squared,  $Q^2$ , and Bjorken  $x$ . In the absence of QED radiation,

$$\begin{aligned} Q^2 &= -q^2 = -(k - k')^2, \\ x &= \frac{Q^2}{2P \cdot q}, \end{aligned}$$

where  $k$  and  $P$  are the four-momenta of the incoming particles and  $k'$  is the four-momentum of the scattered lepton. The fraction of the lepton energy transferred to the proton in its rest frame is  $y = (P \cdot q)/(P \cdot k) = Q^2/(sx)$ , where  $s$  is the square of the total centre-of-mass energy of the lepton-proton collision. The invariant mass of the

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<sup>1</sup> Data on  $F_2^{em}$  based on similar statistics and in a similar kinematic range have recently been presented by the H1 collaboration [2, 3].

hadronic final state,  $W$ , is calculated from

$$W^2 = Q^2 \frac{1-x}{x} + m_p^2,$$

where  $m_p$  is the proton mass.

The double-differential cross section for inclusive  $e^+p$  scattering is given in terms of the structure functions  $F_i$ :

$$\begin{aligned} \frac{d^2\sigma^{e^+p}}{dx dQ^2} &= \frac{2\pi\alpha^2}{xQ^4} [Y_+F_2(x, Q^2) - Y_-xF_3(x, Q^2) - y^2F_L(x, Q^2)] (1 + \delta_r(x, Q^2)) \quad (1) \\ &= \frac{d^2\sigma_{\text{Born}}^{e^+p}}{dx dQ^2} (1 + \delta_r(x, Q^2)), \end{aligned}$$

where  $Y_{\pm} = 1 \pm (1-y)^2$  and  $x$  and  $Q^2$  are defined at the hadronic vertex. In this equation,  $F_L$  is the longitudinal structure function,  $xF_3$  is the parity-violating term arising from  $Z^0$  exchange and  $\delta_r$  is the electroweak radiative correction. The double-differential Born cross section,  $d^2\sigma_{\text{Born}}/dx dQ^2$ , is evaluated using  $1/\alpha = 137.03599$ ,  $\sin^2\theta_W = 0.23147$  and  $M_Z = 91.1882$  GeV [4] to determine the electroweak parameters [5].

The structure function  $F_2$  contains contributions from both virtual photon and  $Z^0$  exchange:

$$F_2 = F_2^{em} + \frac{Q^2}{(Q^2 + M_Z^2)} F_2^{int} + \frac{Q^4}{(Q^2 + M_Z^2)^2} F_2^{wk} = F_2^{em} (1 + \Delta_{F_2}), \quad (2)$$

where  $M_Z$  is the mass of the  $Z^0$  and the contributions to  $F_2$  from photon exchange ( $F_2^{em}$ ),  $Z^0$  exchange ( $F_2^{wk}$ ) and the  $Z^0 - \gamma$  interference term ( $F_2^{int}$ ) are separately indicated. All three contributions are included in the reduced cross section,  $\tilde{\sigma}^{e^+p}$ , defined as:

$$\tilde{\sigma}^{e^+p} = \left[ \frac{2\pi\alpha^2}{xQ^4} Y_+ \right]^{-1} \frac{d^2\sigma_{\text{Born}}^{e^+p}}{dx dQ^2}.$$

### 3 Experimental conditions

The data presented here were taken in 1996 and 1997 using the ZEUS detector at HERA. In this period HERA operated with 174-177 bunches of 820 GeV protons and 27.5 GeV positrons, which collided every 96 ns. Additional unpaired positron, unpaired proton and empty bunches were used to determine beam-related backgrounds. The proton bunch length was approximately 11 cm (r.m.s.) while the positron bunch length was negligible in comparison. Variations of the mean interaction position (from run to run) lead to an

effective length of the interaction region of 11.5 cm (r.m.s.) centred<sup>2</sup> around  $Z = -0.5$  cm. Approximately 6% of the proton current was contained in satellite bunches, which were shifted by  $\pm 4.8$  ns with respect to the nominal bunch crossing time, resulting in a fraction of the  $ep$  interactions occurring at  $\langle Z \rangle \simeq \pm 72$  cm.

A brief outline of the components which are most relevant for this analysis, as illustrated in Fig. 1, is given below. The uranium-scintillator calorimeter (CAL) [6] covers 99.7% of the total solid angle. It consists of the barrel calorimeter (BCAL), covering the polar angle range  $36.7^\circ < \theta < 129.1^\circ$ , the forward calorimeter (FCAL), covering  $2.6^\circ < \theta < 36.7^\circ$  and the rear calorimeter (RCAL), covering  $129.1^\circ < \theta < 178.5^\circ$ . The FCAL and RCAL are divided vertically into two halves to allow temporary retraction during beam injection. The CAL is segmented into electromagnetic (EMC) and hadronic (HAC) sections. Each section is further subdivided into cells of typically  $5 \times 20$  cm<sup>2</sup> ( $10 \times 20$  cm<sup>2</sup> in the RCAL) for the EMC and  $20 \times 20$  cm<sup>2</sup> for the HAC sections. Each cell is viewed by two photomultiplier tubes (PMTs). Under test beam conditions, the calorimeter has a single particle energy resolution of  $\sigma/E = 18\%/\sqrt{E(\text{GeV})}$  for electrons and  $\sigma/E = 35\%/\sqrt{E(\text{GeV})}$  for hadrons [6]. The timing resolution of a calorimeter cell is better than 1 ns for energy deposits greater than 4.5 GeV. To minimise the effects of noise coming from the uranium radioactivity, all EMC (HAC) cells with an energy deposit of less than 60 (110) MeV were discarded in the analysis. For the remaining cells with no neighbouring energy deposits, this cut was increased to 100 (160) MeV.

A presampler (PRES) [7] is mounted in front of FCAL and RCAL. It consists of scintillator tiles that detect particles originating from showers in the material between the interaction point and the calorimeter. This information is used to correct the energy of the scattered positron.

The tracking system consists of a central tracking chamber (CTD) [8] and a rear tracking detector (RTD) [9] enclosed in a 1.43 T solenoidal magnetic field. The interaction vertex was measured with a typical resolution along (transverse to) the beam direction of 0.4 (0.1) cm. The CTD was used to measure track momenta with a resolution of  $\sigma(p_t)/p_t = 0.0058p_t \oplus 0.0065 \oplus 0.0014/p_t$  ( $p_t$  in GeV) and to extrapolate tracks onto the face of the calorimeter with a resolution of 0.3 cm.

The position of positrons scattered at small angles to the positron beam direction was measured using the small angle rear tracking detector (SRTD) [10], which is attached to the front face of the RCAL. The SRTD consists of two planes of scintillator strips, 1 cm wide and 0.5 cm thick, arranged in orthogonal directions and read out via optical fibres

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<sup>2</sup> The ZEUS coordinate system is a right-handed Cartesian system, with the  $Z$  axis pointing in the proton beam direction, referred to as the “forward direction”, and the  $X$  axis pointing left towards the centre of HERA. The coordinate origin is at the nominal interaction point.

and photomultiplier tubes. It covers the region of about  $68 \times 68 \text{ cm}^2$  in  $X$  and  $Y$  and is positioned at  $Z = -148 \text{ cm}$ . A hole of  $8 \times 20 \text{ cm}^2$  at the centre of the RCAL and SRTD accommodates the beampipe. The SRTD signals resolve single minimum-ionising particles and provide a transverse position resolution of 3 mm. The time resolution is better than 2 ns for a minimum-ionising particle. The RTD was used to determine accurately the position of the SRTD.

The hadron-electron separator (HES) [9] consists of a layer of silicon pad detectors. The rear HES is located in the RCAL at a depth of 3.3 radiation lengths. Each silicon pad has an area of  $28.9 \times 30.5 \text{ mm}^2$ , providing a spatial resolution of about 9 mm for a single hit pad. If more than one adjacent pad is hit by a shower, a cluster consisting of at most  $3 \times 3$  pads around the most energetic pad is considered, giving a positron position resolution of 5 mm.

The luminosity was measured via the bremsstrahlung process,  $ep \rightarrow e\gamma p$ , using a lead-scintillator calorimeter (LUMI) [11] which detects photons at angles  $\leq 0.5 \text{ mrad}$  with respect to the positron beam direction. The LUMI photon calorimeter was also used to tag photons from initial-state radiation in DIS events. It was positioned at  $Z = -107 \text{ m}$  and had an intrinsic energy resolution of  $\sigma/E = 18\%/\sqrt{E(\text{GeV})}$ . The carbon-lead filter, placed in front of the calorimeter to shield it from synchrotron radiation, degraded its energy resolution somewhat. The position resolution was 0.2 cm in  $X$  and  $Y$ . In addition, an electromagnetic calorimeter (positron tagger) positioned at  $Z = -35 \text{ m}$  was used for tagging positrons scattered at very small angles.

## 4 Trigger

For the ‘high- $Q^2$  region’ ( $Q^2 \geq 30 \text{ GeV}^2$ ), the data analysed correspond to an integrated luminosity of  $30.6 \pm 0.5 \text{ pb}^{-1}$ . For the ‘low- $Q^2$  region’ ( $Q^2 \geq 2 \text{ GeV}^2$ ), where the positrons are scattered through smaller angles, the data set corresponds to an integrated luminosity of  $2.23 \pm 0.02 \text{ pb}^{-1}$ , which was obtained in short dedicated running periods.

Events were selected online by a three-level trigger system [9]. At the first level (FLT) [12], events with a positron candidate were selected by the logical OR of the following conditions:

- total EMC energy deposit in the BCAL greater than 4.8 GeV;
- total EMC energy deposit in the RCAL, excluding the ring of  $20 \times 20 \text{ cm}^2$  towers closest to the rear beampipe, greater than 3.4 GeV;
- an isolated positron condition (ISO-e) in the RCAL. The ISO-e condition requires that the isolated EMC energy deposit be greater than 2.08 GeV and that the HAC

energy behind it be either less than 0.95 GeV or no more than one third of the EMC energy. The isolation criterion required all towers adjacent to the EMC energy deposit associated with the positron to have energy deposits less than 2.08 GeV in the EMC and 0.95 GeV in the HAC. Additionally, the total energy deposit in CAL was required to be greater than 0.464 GeV and a signal above threshold was required in the SRTD;

- total transverse energy in the CAL greater than 30 GeV;
- total transverse energy in the CAL greater than 11.6 GeV and at least one track candidate in the CTD;
- total EMC energy deposit in the CAL greater than 10 GeV and at least one track candidate in the CTD.

Backgrounds from protons interacting outside the detector were rejected using the time measurement of the energy deposits in upstream veto counters and in the SRTD.

The trigger efficiency of the FLT for events that passed the offline selection cuts (see Section 9.1) was greater than 99%, as determined from dedicated trigger studies and from Monte Carlo (MC) simulations.

The second-level trigger (SLT) further reduced the background using the times measured in the calorimeter cells and the summed energies from the calorimeter. Energy and momentum conservation require  $ep$ -collisions to conserve  $\delta$ :

$$\delta = E - P_Z = \sum_i E_i(1 - \cos \theta_i). \quad (3)$$

In this equation,  $E_i$  and  $\theta_i$  are the energies and polar angles of all energy deposits in the CAL. For perfect detector resolution and for fully contained DIS events,  $\delta$  will equal twice the positron beam energy (55 GeV). For photoproduction events, where the scattered positron escapes down the beampipe,  $\delta$  peaks at much lower values. Proton beam-gas events that originate from inside the detector have energy concentrated in the forward direction and so also have small values of  $\delta$ .

The events were accepted at the SLT if they satisfied the condition that

$$\delta_{SLT} = \sum_i E_i(1 - \cos \vartheta_i) > (29 \text{ GeV} - 2E_\gamma)$$

where  $\vartheta_i$  is the polar angle of the energy deposit with respect to the nominal vertex and  $E_\gamma$  is the energy deposit measured in the LUMI photon calorimeter.

The full event information was available at the third-level trigger (TLT). Tighter timing cuts as well as algorithms to remove beam-halo muons and cosmic rays were applied. The quantity  $\delta_{TLT}$  was determined using the reconstructed vertex and the events were required to have  $\delta_{TLT} > (30 \text{ GeV} - 2E_\gamma)$ . Finally, events were accepted if a scattered positron

candidate with energy greater than 4 GeV was found. To ensure full containment of the shower in the calorimeter, events in which the scattered positron was located within 2 cm of the beamhole were rejected.

In total 1,747,944 (3,935,516) NC DIS candidates satisfied the above low- $Q^2$  (high- $Q^2$ ) trigger condition.

## 5 Reconstruction of event kinematics

In the determination of the event kinematics, the CAL energy deposits were separated into two categories: those associated with the identified scattered positron, and all other energy deposits. The latter were defined as the hadronic energy. The kinematics of the event was then determined from:

- the energy ( $E'_e$ ) and polar angle ( $\theta_e$ ) of the scattered positron;
- the hadronic energy expressed in terms of the longitudinal:

$$\delta_h = \sum_h (E_h - P_{Z,h})$$

and transverse:

$$P_{T,h} = \sqrt{(\sum_h P_{X,h})^2 + (\sum_h P_{Y,h})^2}$$

components, where the sums run over all energy deposits not associated with the scattered positron.

The hadronic energy flow is characterised by an angle  $\gamma_h$  defined by:

$$\cos \gamma_h = \frac{P_{T,h}^2 - \delta_h^2}{P_{T,h}^2 + \delta_h^2}. \quad (4)$$

In the quark-parton model, the angle  $\gamma_h$  corresponds to the polar angle of the struck quark.

The following refinements in the calculation of  $\gamma_h$  were applied in order to optimise the accuracy and precision of the reconstruction:

- the transverse momentum of the hadronic system,  $P_{T,h}$ , was replaced by the more accurately measured transverse momentum of the scattered positron,  $P_{T,e}$ ;
- at low values of  $\delta_h$ , part of the hadronic system escapes detection through the forward beamhole. A parameterisation, determined from MC simulation, as a function of the measured ratio  $P_{T,h}/P_{T,e}$ ,  $\gamma_h$  and  $Q^2$  was used to correct  $\delta_h$ :

$$\delta_{h,\text{cor}} = \delta_h \mathcal{C}(P_{T,h}/P_{T,e}, \gamma_h, Q^2); \quad (5)$$

- in the determination of  $y$  at large values of  $\delta_h$ , the information from the positron provides the most accurate measurement,  $y_e = 1 - (E'_e/2E_e)(1 - \cos \theta_e)$ . However, at low values of  $\delta_h$ , the hadronic information provides a more accurate measurement,  $y_{\text{cor}} = \delta_{h,\text{cor}}/(2E_e)$ . The  $\Sigma$ -correction [13] combines  $y_{\text{cor}}$  and  $y_e$  such that

$$y_{\Sigma,\text{cor}} = \frac{\delta_{h,\text{cor}}y_e + \delta_e y_{\text{cor}}}{\delta_e + \delta_{h,\text{cor}}},$$

where  $\delta_e = E'_e(1 - \cos \theta_e)$ ;

- finally,  $\gamma_{\text{PT}}$  was calculated from:

$$\cos \gamma_{\text{PT}} = \frac{P_{T,e}^2 - \delta_{\Sigma,\text{cor}}^2}{P_{T,e}^2 + \delta_{\Sigma,\text{cor}}^2}, \quad (6)$$

where  $\delta_{\Sigma,\text{cor}} = 2E_e y_{\Sigma,\text{cor}}$ .

For the present analysis, the PT method [1] was used to reconstruct the kinematic variables of the events:

$$\begin{aligned} Q_{\text{PT}}^2 &= 4E_e^2 \frac{\sin \gamma_{\text{PT}}(1 + \cos \theta_e)}{\sin \gamma_{\text{PT}} + \sin \theta_e - \sin(\gamma_{\text{PT}} + \theta_e)}; \\ x_{\text{PT}} &= \frac{E_e \sin \gamma_{\text{PT}} + \sin \theta_e + \sin(\gamma_{\text{PT}} + \theta_e)}{E_p \sin \gamma_{\text{PT}} + \sin \theta_e - \sin(\gamma_{\text{PT}} + \theta_e)}; \\ y_{\text{PT}} &= \frac{Q_{\text{PT}}^2}{sx_{\text{PT}}}; \\ W_{\text{PT}}^2 &= Q_{\text{PT}}^2 \frac{1 - x_{\text{PT}}}{x_{\text{PT}}} + m_p^2. \end{aligned}$$

This reconstruction method achieves good resolution and minimises biases in  $x$  and  $Q^2$  over the full kinematic range.

## 6 Monte Carlo simulation

Monte Carlo (MC) event simulation was used to correct for detector acceptance and resolution effects. The detector simulation is based on the GEANT program [14] and incorporates the best understanding of the detector and the trigger, including test beam results. Neutral current DIS events were simulated with radiative effects using the HERACLES 4.5.2 [15] program interfaced to the LEPTO 6.5 [16] MC program by the DJANGO6 2.4 program [17]. HERACLES includes  $\mathcal{O}(\alpha)$  leptonic corrections for initial- and final-state radiation, and one-loop vertex and propagator corrections. In addition, leading logarithmic effects to order  $\mathcal{O}(\alpha\alpha_s)$  are included. The hadronic final state was simulated

using the colour-dipole model CDMBGF [18] including all leading-order QCD diagrams as implemented in ARIADNE 4.08 [19] for the QCD cascade and JETSET 7.4 [20] for the hadronisation. The ARIADNE model provides the best description of the characteristics of the DIS non-diffractive hadronic final state [21]. Diffractive events which are characterised by a large rapidity gap in the detector [22, 23] were simulated within ARIADNE, which was interfaced to the RAPGAP 2.06/52 [24] program. The latter assumes that the struck quark belongs to a colourless state having only a small fraction of the proton momentum. The diffractive and non-diffractive samples were mixed as a function of  $x_{\text{PT}}$  and  $Q_{\text{PT}}^2$  as determined from the  $\eta_{\text{max}}$  distribution in the data, where  $\eta_{\text{max}}$  is the pseudorapidity of the most forward energy deposit with more than 400 MeV. The overall normalisation was kept fixed. The CTEQ4D [25] parton density parameterisations were used in the simulations.

The vertex distribution used in the simulation was taken from DIS events having both scattered positrons and hadrons well reconstructed by the CTD. The vertex finding efficiency is well described by the MC simulation, as is shown below (see Section 7.1).

The effects of the uranium radioactivity were studied in randomly triggered events. The energy deposits in these events originate entirely from the calorimeter noise. The rate and energy distribution were simulated in the MC program.

Twelve different MC samples with varying  $Q^2$  ranges were generated with integrated luminosities increasing with  $Q^2$ , from  $1.2 \text{ pb}^{-1}$  for  $Q^2 > 0.5 \text{ GeV}^2$  to  $1500 \text{ fb}^{-1}$  for  $Q^2 > 40000 \text{ GeV}^2$ . The fluctuations in the final result due to the MC sample statistics are small.

The main source of background in the data comes from photoproduction interactions that led to the detection of a fake scattered positron. Resolved and direct photoproduction events [26] were simulated using PYTHIA 5.724 [20], with the total cross section given by the ALLM parameterisation [27]. Resolved and direct photoproduction events, corresponding to integrated luminosities of  $0.7$  and  $2.5 \text{ pb}^{-1}$ , respectively, were generated with  $y > 0.36$ . Events with smaller  $y$  values do not contribute to the photoproduction background due to the requirement on  $\delta$ .

## 7 Positron identification and measurement

The positron-identification algorithm is based on a neural network using information from the CAL [28]. The network separates energy deposits in the calorimeter that are due to electromagnetic showers from those that are of hadronic origin by assigning a ‘positron-probability’ value. If more than one positron is identified, the one with the highest probability is taken to be the scattered positron. Monte Carlo studies show that



the efficiency for finding the scattered positron increases from 70% at 8 GeV to greater than 99% for energies above 25 GeV. This was checked by using QED-Compton events. The results obtained from the neural network were compared to an alternative positron-finding algorithm [29]. Systematic differences of the order of 2% were observed at 8 GeV, decreasing to less than 1% for energies higher than 15 GeV.

## 7.1 Positron angle measurement

The scattering angle of the positron was determined using either its impact position on the CAL inner face and the event vertex or from a reconstructed track in the CTD. For  $\theta_e \lesssim 150^\circ$ , the scattered positron registers in the three innermost superlayers of the CTD and the parameters of the reconstructed track, matched to the positron impact position, were used.

For  $\theta_e \gtrsim 150^\circ$ , the impact position of the scattered positron on the inner face of the calorimeter was reconstructed using other detector elements. The SRTD information was used, when available; otherwise the HES information was used. If neither HES nor SRTD information was available, then the CAL reconstruction was used:

- SRTD – the positron position in the SRTD was determined from the centres of gravity of the pulse-heights of the strips in the  $X$  and  $Y$  planes of the SRTD. The measured position resolution was 3 mm. For a subset of these positrons, the position measured by the SRTD was compared to the result from the track measurement. The resolution of the RTD-SRTD matching was 3 mm and systematic deviations were less than 1 mm;
- HES – the position in the HES was determined from the pulse-height sharing in the pads. The position measurement was checked by matching tracks and positron candidates. The resolution of the track-HES matching was 5 mm with systematic deviations smaller than 1.5 mm;
- CAL – the position of a shower in the CAL was determined using the relative pulse-height of the left and right PMTs and energy deposits in neighbouring cells. The position resolution on the face of the CAL was about 10 mm. The alignment of the calorimeter was checked by matching tracks and positron candidates in the CAL. The resolution of the track-CAL matching was 10 mm with systematic biases of less than 2 mm.

The coordinates of the event vertex were determined from tracks reconstructed with the CTD. The  $Z$  coordinate ( $Z_{\text{vertex}}$ ) was determined on an event-by-event basis. However, since the transverse sizes of the beams were smaller than the resolutions for the  $X$  and  $Y$  coordinates, the average  $X$  and  $Y$  vertex positions per beam fill were used. For events

not having a tracking vertex, the  $Z$  coordinate was set to  $Z = 0$ , the nominal position of the interaction point averaged over all runs.

The probability of finding a vertex depended on the number of particles detected in the tracking detectors and thus mainly on the hadronic angle,  $\gamma_h$ . Figure 2 shows the fraction of events having a reconstructed vertex as a function of  $\gamma_{PT}$ . For  $\gamma_{PT} > 70^\circ$ , the vertex efficiency was greater than 95%. In the low- $Q^2$  sample, it decreased to about 50% for events with  $\gamma_{PT} \sim 20^\circ$ . The MC simulation reproduces the observed behaviour well. The drop in vertex-finding efficiency near  $\gamma_{PT} = 174^\circ$  results from the combination of the characteristics of the DIS final states and the acceptance of the CTD in the rear direction. At low  $\gamma_{PT}$ , the vertex-finding efficiency is higher for high- $Q^2$  events, since the scattered positron is detected more often by the CTD.

The  $Z$  coordinate of the vertex can also be determined from the measurements of the arrival times of energy deposits in the FCAL. The corresponding resolution is  $\sigma_Z^{\text{timing}} = 9$  cm. This determination was only used for studies of systematic uncertainties.

For polar angles  $17.2^\circ \lesssim \theta_e \lesssim 150^\circ$  and positron momenta  $> 5$  GeV, the tracking efficiency was greater than 98%. Thus, when the impact position on the CAL inner face was outside a radius of 80 cm around the beampipe, corresponding to a scattering angle of  $150^\circ$  for events with  $Z = 0$ , a track was required to match the positron identified in the CAL and the polar angle was taken from the track parameters. A successful match required that the distance between the extrapolated impact point of the track on the face of the CAL and the position determined by the CAL was less than 10 cm.

The resolution of the scattering-angle measurement was  $\sigma_{\theta_e}^{\text{SRTD}} \simeq 2.0$  mrad for positrons reconstructed in the SRTD,  $\sigma_{\theta_e}^{\text{HES}} \simeq 3.4$  mrad for positrons measured in the HES,  $\sigma_{\theta_e}^{\text{CAL}} \simeq 6.8$  mrad for positrons measured in the CAL and  $\sigma_{\theta_e}^{\text{track}} \simeq 2.6$  mrad for positrons with a matched track.

## 7.2 Positron energy determination

The scattered positron loses energy in the passive material in front of the CAL. In the region used for this analysis, this corresponds to about 1.2 radiation lengths except in areas around the rear beampipe,  $\theta \gtrsim 170^\circ$ , and the solenoid support structure,  $130^\circ \lesssim \theta \lesssim 145^\circ$ , where it corresponds to 2.0 and 2.5 radiation lengths, respectively. In the analysis, the CAL measurement of the scattered positron energy was corrected for these energy losses.

The correction was determined directly from the data using the following subsamples:

- at low  $y$ , the scattered positron energy is kinematically constrained to be close to the positron beam energy and to be primarily a function of the scattering angle. For these events, called kinematic peak (KP) events, the mean positron energy can be

determined from the scattering angle ( $E'_e \approx 2E_e/(1 - \cos \theta_e)$ ) to within 0.5%. The KP events were selected by requiring  $y_{JB} = \delta_h/(2E_e) < 0.04$  [30], and provide an energy calibration at  $E'_e \approx E_e = 27.5$  GeV for  $\theta \gtrsim 135^\circ$ ;

- the double angle (DA) method [31] predicts the positron energy from the angular information of the scattered positron and the hadrons,  $E'_e = (2E_e \sin \gamma_h)/(\sin \gamma_h + \sin \theta_e - \sin(\gamma_h + \theta_e))$ . This relation was used to relate the energy loss in passive material to the SRTD and PRES signal, in the energy range  $15 \lesssim E'_e \lesssim 25$  GeV, assuming no hard QED radiation in the initial state;
- for QED Compton events ( $ep \rightarrow e\gamma p$ ) observed in the main detector, the energies of the positron and the photon can be predicted precisely from the measurement of their scattering angles since the transverse momentum of the scattered proton is small. QED Compton events provide a calibration for  $5 \lesssim E'_e \lesssim 20$  GeV and  $\theta \gtrsim 160^\circ$ ;
- in the range  $17.2^\circ \lesssim \theta \lesssim 150^\circ$ , the momenta of the positrons can be independently determined from the CTD.

For scattered positrons in the RCAL, the correlation between the energy lost in the passive material in front of the calorimeter and the energy deposited in the SRTD or presampler was used to correct the calorimeter energy measurement. The corrections were determined using the KP and DA samples. The QED Compton events were used as a check on the correction.

The uncertainty in the energy determination, after all corrections, was 2% at 8 GeV, falling linearly to 1% at 15 GeV. In the region covered by BCAL and FCAL,  $\theta \lesssim 130^\circ$ , the positron cluster energy was corrected based on material maps implemented in the detector simulation package. For scattered positrons in the BCAL [29] and RCAL, the corrections for non-uniformities due to geometric effects caused by cell and module boundaries were also made. Identical studies were also performed on the event samples generated by the MC simulations. The resulting corrections were applied to the events generated in the MC simulation.

## 8 Hadronic energy determination

Energy deposits coming from the hadronic final state were used to evaluate the quantities  $\delta_h$  and  $P_{T,h}$ . These energy deposits, unlike those of the positron, were not corrected for energy loss in the passive material. Instead, a combination of clusters of energy deposits in the CAL and the corresponding tracks measured in the CTD were used in determining the hadronic energy [32]. The selected calorimeter clusters and tracks are referred to as energy flow objects (EFOs). The use of track information reduces the sensitivity to

energy losses in inactive material in front of the CAL. However, the energies of particles for which no track information was available (e.g., because the energy was deposited by a neutral particle) were measured using the CAL alone.

Monte Carlo studies of the calorimeter response indicated that the uncorrected  $\gamma_h$  calculated with Eq. (4) was biased by hadronic energy coming from interactions in material between the primary vertex and the calorimeter or by backsplash from the calorimeter (albedo), primarily from the FCAL. To minimise this bias, neutral clusters with energy below 3 GeV and with polar angles larger than a  $\gamma_{\max}$ ,  $\gamma_{\max} = \gamma_h + 50^\circ$ , were removed on an event-by-event basis. The choice of  $50^\circ$  was derived from the MC simulation by minimising the dependence of  $\delta_h$  on  $\gamma_{\max}$ . For the values of  $\gamma_{\max}$  used, the biases in  $\delta_h$  and  $P_{T,h}$  were small. The agreement of the distributions of removed energies for different  $\gamma_h$  ranges between data and MC simulation was also good. After a first pass of cluster removal, the value of  $\gamma_h$  was re-calculated and the procedure repeated until it converged, typically after two or three iterations. Removing calorimeter clusters in this manner substantially improved the resolution and reduced the bias of the quantities  $\delta_h$  and  $P_{T,h}$  at low values of  $\delta_h$  (corresponding to small values of  $y$ ) and left them largely unchanged for large values of  $\delta_h$ .

The transverse momentum of the positron,  $P_{T,e}$ , calculated using the positron energy, corrected as described in the previous section, was compared to the  $P_{T,h}$  of the hadrons in both the MC simulation and the data. Uncertainties in the determination of the hadronic energy were estimated from this comparison. The Monte Carlo simulation of the mean  $P_{T,h}/P_{T,e}$  as a function of  $\gamma_h$  agrees within 2% with the data for the entire kinematic range covered in this paper. Based on these comparisons, an uncertainty of  $\pm 2\%$  was assigned to the hadronic-energy measurement, neglecting the uncertainty due to the angular information in the calculation of  $P_{T,h}$ , which is small.

## 9 Data sample

### 9.1 Event selection

The following cuts, using the energy and angle of the scattered positron, were used both to select NC DIS events and to reject background:

- a positron candidate, defined as described in Section 7;
- $E'_e > 8$  GeV, where  $E'_e$  is the corrected positron energy. This cut ensured high and well understood positron finding efficiency and suppressed background from photoproduction;

- events with an impact point of the scattered positron on the RCAL inside a box of  $26 \times 14 \text{ cm}^2$  centred around the beampipe were rejected (“box cut”). This ensured that the impact point was at least 2.5 cm away from the edge of the RCAL and therefore guaranteed full containment of the electromagnetic shower in the calorimeter. Events in which the scattered positron traversed the rear cooling pipes around the beampipe were also rejected. In the high- $Q^2$  sample, events with an impact point of the scattered positron on the RCAL inside a radius of 28 cm around the beampipe were also rejected;
- a track match for  $17.2^\circ < \theta_e \lesssim 150^\circ$ . This condition suppressed events from cosmic rays, halo-muons, photoproduction and DIS events in which an electromagnetic shower was falsely identified as the scattered positron;
- to reduce photoproduction background further, isolated positrons were selected by requiring no more than a total of 5 GeV from all calorimeter cells not associated with the scattered positron in an  $\eta - \phi$  cone of radius 0.8 centred on the positron.

The hadronic information was used in the following selection criteria:

- $38 < \delta < 65 \text{ GeV}$ , where  $\delta = \sum_i (E_i - P_{Zi})$ . Here the sum runs over both the energy flow objects from the hadronic system and the energy deposits belonging to the identified positron. This cut removed events with large initial-state radiation and further reduced the background from photoproduction. For events with a scattered positron beyond the tracking acceptance ( $\theta_e < 17.2^\circ$ ), the minimum requirement was raised to  $\delta > 44 \text{ GeV}$ ;
- $P_{T,h}/P_{T,e} > 0.3$ . For the PT method to yield a reliable measurement of  $x$  and  $Q^2$ , the loss of hadronic transverse momentum must be small. In some events, a substantial part of the current jet remained in the forward beampipe. These events, produced at small  $\gamma_h$ , could be falsely reconstructed at large  $\gamma_h$  due to the CAL noise or backslash. This cut suppressed such events.

Finally, the following cuts were applied:

- $y_e < 0.95$ . This condition removes events where fake positrons are found in the FCAL;
- $-50 \text{ cm} < Z_{\text{vertex}} < 50 \text{ cm}$ . This cut was applied to events with a reconstructed tracking vertex; it suppressed beam-gas background events and the small fraction of the events in which the vertex position was incorrectly measured. Events without a tracking vertex were accepted and were assigned the mean vertex  $Z$  position;
- $W_{\text{PT}} > 20 \text{ GeV}$ . This cut, corresponding to  $y \gtrsim 0.004$  for  $Q^2 \lesssim 400 \text{ GeV}^2$ , selected the kinematic region where a reliable measurement could be made. Events below this cut failed the acceptance and purity requirements described in Section 9.2. At low  $W$ , the hadronic system is partially lost in the forward beampipe and therefore the measurements are sensitive to the detailed simulation of the beampipe region.

A total of 561,405 (1,300,887) events passed the low (high)  $Q^2$  selection cuts.

## 9.2 Binning and resolution

The relative resolution in  $x$  improves from approximately 35% at  $y \sim 0.005$ , to  $\sim 11\%$  for  $y > 0.1$ . The relative resolution in  $Q^2$  is  $\sim 2\%$  for  $y \sim 0.1$  and deteriorates to approximately 5% at  $y \gtrsim 0.5$  and  $\sim 10\%$  at  $y \lesssim 0.01$ . For  $Q^2 > 400 \text{ GeV}^2$ , the  $Q^2$  relative resolution is approximately 2.5%.

The  $(x, Q^2)$ -bins used for the determination of the structure function are shown in Fig. 3. The numbers of events in each of the bins are given in Table 1. The bins were chosen commensurate with the resolutions. At large  $Q^2$  and also at low  $y$ , larger bin sizes were chosen to obtain adequate statistics in each bin and to minimise bin-to-bin migrations as a result of the non-Gaussian tails. Furthermore, good acceptance ( $A > 20\%$ ) and purity ( $P > 30\%$ ) were required for each bin. The acceptance was defined as the fraction of events generated in a bin that passed the event selection. The purity was defined as the fraction of events reconstructed in a bin that were generated in that bin. The lowest values of acceptance occur at the lowest  $Q^2$  values where the box cut (see Section 9.1) becomes effective. The bins with lowest purity occur at the lowest  $y$  values. In the majority of bins, the acceptance is greater than 80% and the purity is greater than 50%, as shown in Fig. 3.

## 9.3 Background estimate

The final sample contains a small number of background events from the following sources:

- **non- $ep$  background.** The background not associated with  $ep$  collisions was determined from the number of events observed in unpaired or empty bunches. This background was subtracted statistically, taking into account the appropriate ratios of bunch currents and numbers of bunches. It is less than 1% for most bins and reaches 3% for a few bins at low  $y$ ;
- **photoproduction background.** The events from the photoproduction MC generator PYTHIA were analysed in the same way as the data and the number of events passing the selection cuts in each bin was determined. This number of events was subtracted. In the region  $\delta < 40 \text{ GeV}$ , the photoproduction contribution was measured directly through events tagged by the positron tagger, as seen in Fig. 4a. The MC photoproduction background sample was normalised to the measurement at  $\delta < 40 \text{ GeV}$  and subtracted bin by bin. The total photoproduction background contribution to

each bin is given in Table 1. The maximum background fraction of about 20% occurs in bins at high  $y$  and low  $Q^2$ .

- **charged current background.** The background from charged current interactions is negligible.

## 9.4 Event characteristics

Figure 5 shows the characteristics of both low- and high- $Q^2$  samples of accepted events. To obtain these distributions, the MC events were reweighted to the structure function obtained from the NLO QCD fit to these data (see Section 10.4). The energy, angular and transverse momentum distributions are well reproduced by the MC simulation (also indicated in the figures).

Figure 6 shows the distributions in  $y_{\text{PT}}$ ,  $x_{\text{PT}}$  and  $Q_{\text{PT}}^2$  together with the MC distributions normalised to the integrated luminosity of the data. Good agreement for the high- $Q^2$  sample is seen.

The discrepancies seen at low  $y$  and low  $Q^2$ ,  $Q^2 \lesssim 15 \text{ GeV}^2$  and  $y \lesssim 10^{-2}$ , are located in three  $(x, Q^2)$ -bins, the highest  $x$  bins at  $Q^2 = 3.5, 6.5$  and  $10 \text{ GeV}^2$ , from a total of 242 bins. The systematic uncertainty in this low- $y$  region (see Section 10.2) is 10%. This discrepancy between data and MC simulation is approximately equal to the systematic uncertainty (not shown in the figure). Reweighting the MC simulation to get agreement in this region does not affect the extracted structure function values.

# 10 Results

## 10.1 Extraction of the proton structure function $F_2^{em}$ and the reduced cross section

Monte Carlo events were generated according to Eq. (1) including QED radiative effects. The value of  $\tilde{\sigma}^{e^+p}$ , at fixed  $(x, Q^2)$  within a bin, was obtained from the ratio of the number of observed events to the number of events predicted from the MC simulation in that bin, multiplied by the reduced cross section from the Monte Carlo generator,  $\tilde{\sigma}_{\text{MC}}^{e^+p}(x, Q^2)$ . The acceptance correction and bin-centering correction are thus taken from the MC simulation. The MC events contain transverse and longitudinal photon and  $Z^0$  contributions, which can be written as  $F_2^{int}$ ,  $F_2^{wk}$ ,  $x F_3$  and  $F_L$  or, equivalently, the *relative* corrections  $\Delta_{F_2}$  (see Eq.(2)),  $\Delta_{x F_3}$  and  $\Delta_{F_L}$  according to:

$$\tilde{\sigma}^{e^+p} = F_2^{em}(1 + \Delta_{F_2} + \Delta_{x F_3} + \Delta_{F_L}) = F_2^{em}(1 + \Delta_{all}). \quad (7)$$

The result for  $F_2^{em}$  was obtained by correcting the reduced cross section,  $\tilde{\sigma}^{e^+p}$ , for these relative contributions,  $\Delta_{all}$ , from the CTEQ4D parton distribution functions [33] used in the MC generation. The reduced cross section and  $F_2^{em}$  results do not significantly change if the NLO QCD fit results, instead of CTEQ4D, are used in the unfolding procedure.

The statistical uncertainties on the reduced cross sections were calculated from the number of events measured in the bins, taking into account the background and the statistical uncertainty from the MC simulation. Poisson statistics was used for the two bins that contain fewer than 5 events.

The reduced cross sections and  $F_2^{em}$  values were corrected for higher-order QED radiative effects not included in HERACLES. These second-order leading-logarithmic corrections, as well as third- and higher-order terms coming from soft-photon exponentiation, were evaluated using the program HECTOR 1.00 [34]. They lie between  $-0.2\%$  and  $-0.5\%$  and vary smoothly with  $Q^2$ . A constant correction of  $-0.35\%$  was applied.

## 10.2 Systematic uncertainties

Several factors contribute to the systematic uncertainties of  $F_2^{em}$  and  $\tilde{\sigma}^{e^+p}$ . The relative uncertainties in  $\tilde{\sigma}^{e^+p}$  are identical to those quoted for  $F_2^{em}$ . Ten sources of systematic uncertainties were found to be correlated between the different  $F_2^{em}$  bins and are denoted by  $\{\}$  in the text and in Table 2.

The ten correlated systematic uncertainties are:

- {1} positron finding and efficiency.

The positron identification efficiency was varied within the uncertainty found in the QED Compton study, which is  $\sim 2\%$  for positron energies  $E'_e \sim 8$  GeV and  $\sim 1\%$  for energies above 15 GeV. The effect on  $F_2^{em}$  is  $\sim 1\%$ , except in the lowest  $x$  bins where it reaches about 2%;

- {2} positron scattering angle - A.

The uncertainty in the alignment of the different detector elements results in a systematic uncertainty in the angle of the scattered positron. The difference between the extrapolated track position at the face of the CAL and the position found from the CAL, the HES or the SRTD shows that this uncertainty was about 2 mm. The largest systematic uncertainty was obtained if the separation between the  $+X$  and  $-X$  halves of the RCAL was changed by  $\pm 2$  mm, resulting in an uncertainty of  $\sim 1\%$  for  $Q^2 \lesssim 200$  GeV<sup>2</sup>;

- {3} positron scattering angle - B.

For positron angles measured with the tracking detector, the scattering angle  $\theta_e$  was



changed by the estimated systematic uncertainty of  $\pm 1$  mrad in the track angle. This change had a 1% effect on the measured  $F_2^{em}$  at high  $Q^2$ ;

{4} positron energy scale.

The systematic uncertainties in  $F_2^{em}$  due to the uncertainties in the absolute calorimeter energy calibration for scattered positrons was estimated by changing the energy scale in the MC simulation: the change is 2% at 8 GeV, linearly decreasing to 1% at 15 GeV (see Section 7.2). Systematic variations of 1% in  $F_2^{em}$  are observed;

{5-7} hadronic energy measurement.

The hadronic energy scales of the different calorimeter regions in the MC simulation were changed by  $\pm 2\%$  in turn for the FCAL {5}, BCAL {6} and RCAL {7}, while leaving the positron energy scale unchanged. The value of 2% is based on detailed comparisons of the distributions of the quantity  $P_{T,h}/P_{T,e}$  from data and MC simulation, see Section 8. The effect on  $F_2^{em}$  was typically 2% in these bins at the highest or lowest  $y$  and about 0.5% elsewhere;

{8} hadronic energy flow - A.

The hadronic energy flow for diffractive events is different from that for non-diffractive events. To investigate the sensitivity of the PT reconstruction method to the size of the diffractive component, the diffractive scattering cross section in the MC simulation was reweighted such that it changed by  $\pm 50\%$  while leaving the correction function  $\mathcal{C}$  (Eq. 5) unchanged. Effects of at most 2% at low  $Q^2$  and high  $y$  in  $F_2^{em}$  are observed. The variations in  $F_2^{em}$  are negligible elsewhere. This is also a check on the effect of different simulations of the hadronic energy flow between the struck parton and the proton remnant;

{9} background subtractions.

As described above, the photoproduction background estimated using the PYTHIA MC simulation agreed with the photoproduction contribution extracted from events tagged by the positron tagger. Uncertainties in the positron-tagger efficiency and in the fake-positron background in the PYTHIA MC simulation led to an overall uncertainty in the photoproduction background of  $\pm 35\%$ , as is indicated in Fig.4b. This resulted in an uncertainty in  $F_2^{em}$  which is at most 11% for  $y \gtrsim 0.4$  and negligible elsewhere;

{10} hadronic energy flow - B.

The hadronic angle  $\gamma_{PT}$  was calculated using the energy and angle of hadronic clusters (see Section 5). The hadronic angle can lie inside the forward beamhole for low- $y$  events, since the energy deposits around the beamhole are merged into one cluster. To estimate the uncertainty in the cluster algorithm and the simulation of the hadronic final state in the forward direction, a summation over energy deposits in calorimeter cells, instead of EFOs, was used in the hadronic reconstruction. Systematic variations

in  $F_2^{em}$  up to 10% were observed in the lowest  $W$  bins, leaving  $F_2^{em}$  at medium and high  $y$  unchanged.

The four uncorrelated systematic uncertainties are:

- 1) positron finding and efficiency.

Varying the isolation criterion requirement of 5 GeV by  $\pm 1$  GeV around an  $\eta - \phi$  cone of radius 0.8 centred on the positron has a negligible effect on  $F_2^{em}$ ;

- 2) positron scattering angle.

Enlarging the box cut, discussed in Section 9.1, by 1 cm in both data and MC simulation had an effect of  $\pm 1$ -3% on  $F_2^{em}$  for low values of  $Q^2 \lesssim 10$  GeV<sup>2</sup> and a negligible effect elsewhere;

- 3) hadronic energy flow - A.

The value of  $\gamma_{\max}$  (see Section 8) was varied by  $\pm 10^\circ$ , hence varying the amount of hadronic energy removed from the event. Only small variations in the bias of  $\delta_h$  were seen in the MC simulation. This reflects the uncertainty in the MC simulation of low-energy deposits in the CAL and the albedo effect. Variations up to 2% in  $F_2^{em}$  were observed in the bins at  $y \lesssim 0.02$ ; elsewhere the variations were within 1%. In the low statistics bins at  $x = 0.65$  and  $Q^2 > 1200$  GeV<sup>2</sup>, this effect increased to  $\sim 10\%$ ;

- 4) hadronic energy flow - B.

The fraction of events removed by the  $P_{T,h}/P_{T,e}$  cut is sensitive to the amount of  $P_{T,h}$  lost in the forward beampipe and thus to the details of the jet and proton-remnant fragmentation. The  $P_{T,h}/P_{T,e}$  cut was varied from 0.3 by  $\pm 0.1$ , which resulted in changes of 1% at low  $y$ .

The systematic uncertainties that did not exhibit a clear correlation were added in quadrature and are listed in Table 2 as  $\delta_{unc}$ .

The satellite bunches were varied in the MC simulation by  $\pm 30\%$  to estimate the uncertainty in the luminosity corresponding to the events in the satellite bunch. Effects on the measured  $F_2^{em}$  were typically 0.5-1% and were included in the normalisation uncertainty.

Both the uncorrelated and correlated contributions to the systematic uncertainty were symmetrised by averaging the positive and negative deviations. For the asymmetric systematic checks, such as the boxcut and the check on the clustering, where only a variation in one direction was applied, the variation of the  $F_2^{em}$  measurement was symmetrised by mirroring the variation.

Figure 7 shows the statistical and systematic uncertainties on  $F_2^{em}$  for each bin as a function of  $y$ . Four contributions to the correlated systematic uncertainty are also shown. The two largest contributions to the correlated systematic uncertainty come from {9} and {10}. Most sources of the systematic uncertainty show a correlation between the

points as a function of  $y$ . The variation of the gap between the two RCAL halves shows a correlation in  $Q^2$ . Figure 8 shows the statistical and total systematic uncertainty in each individual bin in the  $(x, Q^2)$ -plane.

The systematic uncertainties presented above do not include the uncertainty in the measurement of the integrated luminosity ( $\pm 1.5\%$ ), the overall trigger efficiency ( $\pm 1.0\%$ ), the higher-order electroweak radiative corrections ( $\pm 0.5\%$ ) or the determination of the vertex distribution ( $\pm 1.0\%$ ). These effects lead to a combined uncertainty of  $\pm 2\%$  on the overall normalisation of  $F_2^{em}$ . An additional  $\pm 1\%$  relative normalisation uncertainty was assigned to the low- $Q^2$  sample to account for the additional uncertainty on the shape of the vertex distribution in the MC simulation.

### 10.3 Reduced cross section and $F_2^{em}$

The values of the reduced cross section  $\tilde{\sigma}^{e^+p}$  and the electromagnetic structure function  $F_2^{em}$  are given in Table 1 together with their statistical ( $\delta_{stat}$ ) and systematic ( $\delta_{sys}$ ) uncertainties, the corrections due to the  $Z^0$  contribution to  $F_2$ ,  $\Delta_{F_2}$ , to the parity-violating component of the  $Z^0$  exchange,  $\Delta_{xF_3}$ , and to the longitudinal structure function,  $\Delta_{F_L}$ , see Eq. (7)<sup>3</sup>. The contribution of  $F_L$  to  $\tilde{\sigma}^{e^+p}$  becomes large towards large values of  $y$ ; the contribution of  $Z^0$  exchange is substantial at large  $Q^2$ .

The  $F_2^{em}$  values are displayed versus  $x$  for fixed values of  $Q^2$  in Figs. 9-12. The structure function is measured with much improved precision with respect to the previous ZEUS results [1]. Also shown is the result of the ZEUS NLO QCD fit described below.

Figures 13 and 14 show the  $F_2^{em}$  values as a function of  $Q^2$  for fixed  $x$ . Scaling violations are observed, which decrease as  $x$  increases. Where the data from the measurements presented here at high  $x$  overlap the  $x$  range covered by fixed target experiments [35–37], the agreement is good, as shown in Fig. 14. The results also agree well with the recently published data of the H1 collaboration [2, 3] and with the recent parameterisations from CTEQ [38] and MRST [39].

The  $Q^2$ -range has increased substantially with respect to previous ZEUS measurements. The ZEUS data in combination with fixed target data now span almost four orders of magnitude in  $Q^2$  at  $x \sim 0.4$ .

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<sup>3</sup> The table with the results and the uncertainties can be obtained from:  
<http://www-zeus.desy.de/publications.php3>

## 10.4 NLO QCD fit

A next-to-leading-order (NLO) QCD fit to the reduced cross section from this analysis has been performed. Apart from the present data, proton-target data from NMC [35], BCDMS [36], and E665 [37] were used. Deuteron-target data were used from NMC [35] and E665 [37], as well as data on the ratio  $F_2^n/F_2^p$  from NMC [40]. The only neutrino results included in the fit are  $xF_3$  data from CCFR [41].

To remain in the kinematic region where pQCD should be applicable, only data with  $Q^2 > 2.5 \text{ GeV}^2$  were included in the fit. The resonance region and the region affected by higher-twist contributions and target mass effects ( $x \gtrsim 0.1$ ,  $Q^2 \lesssim 20 \text{ GeV}^2$ ) were avoided by requiring  $W^2 > 20 \text{ GeV}^2$ .

The parameterisations of the parton density functions (PDFs) were assumed to have the following functional form, adapted from MRST [39]:

$$xf(x, Q_0^2) = Ax^\delta(1-x)^\eta(1+\gamma x)$$

and were evaluated at  $Q_0^2 = 7 \text{ GeV}^2$ . The  $x^\delta$  term parameterises the steep rise at low  $x$ , whereas  $(1-x)^\eta$  describes the shape of the valence quarks at high  $x$ .

The fit was done in the  $\overline{\text{MS}}$  scheme with a variable-flavour-number *ansatz* (RT-VFN) [42]. A charm mass of 1.35 GeV was assumed. The strange quark distribution,  $x(s(x) + \bar{s}(x)) = 2x\bar{s}(x)$ , was fixed to 0.20 of the total sea, according to measurements of CCFR [43]. The value of  $\alpha_S$  was fixed to the world average value,  $\alpha_S(M_Z^2) = 0.118$ .

The QCD NLO fit reproduces the data over the full kinematic range, indicating that NLO DGLAP evolution can give a consistent description. The overall  $\chi^2/\text{ndf}$  of the fit is 0.95 for 1263 data points, where the  $\chi^2$  is calculated using the statistical and total systematic uncertainty added in quadrature. The  $\chi^2/\text{ndf}$  for the present data is 0.84 for the 242 ZEUS data points.

## 11 Conclusions

Measurements of the reduced cross section and the proton structure function,  $F_2^{em}$ , have been presented from an analysis of inelastic positron-proton neutral current scattering data. The data were taken with the ZEUS detector at HERA during 1996 and 1997. The structure function  $F_2^{em}$  has now been measured over a substantially larger phase space than covered by previous ZEUS measurements and with statistical and systematic uncertainties below 2% in most of the  $(x, Q^2)$  region covered. The data cover  $Q^2$  values between 2.7 and 30000  $\text{GeV}^2$  and  $x$  values between  $6 \cdot 10^{-5}$  and 0.65.

At large  $x$  values and  $Q^2$  values up to 70 GeV<sup>2</sup>, where the new data reach the  $x$ -range covered by fixed-target experiments, good agreement with these experiments is found. There is also good agreement with the data of the H1 collaboration. Strong scaling violations are observed for  $x < 0.02$ . The measured  $x$ - $Q^2$  behaviour of  $F_2^{em}$  can be described by QCD using NLO DGLAP evolution over the full kinematic range.

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## References

- [1] ZEUS Collab., M. Derrick et al., *Z. Phys.* **C 72**, 399 (1996).
- [2] H1 Collab., C. Adloff et al., *Eur. Phys. J.* **C 13**, 609 (2000).
- [3] H1 Collab., C. Adloff et al., Preprint DESY-00-181 (hep-ex/0012053), 2000.  
Accepted by *Eur. Phys. J. C*.
- [4] Particle Data Group, D.E. Groom et al., *Eur. Phys. J.* **C15**, 73 (2000).
- [5] J. Blümlein and M. Klein, in *Proc. Workshop on Physics at HERA, Oct. 1991*, eds. W. Buchmüller and G. Ingelman, Vol. 1, p. 101. Hamburg, Germany, DESY, 1992.
- [6] M. Derrick et al., *Nucl. Instr. and Meth.* **A 309**, 77 (1991);  
A. Andresen et al., *Nucl. Instr. and Meth.* **A 309**, 101 (1991);  
A. Caldwell et al., *Nucl. Instr. and Meth.* **A 321**, 356 (1992);  
A. Bernstein et al., *Nucl. Instr. and Meth.* **A 336**, 23 (1993).
- [7] A. Bamberger et al., *Nucl. Instr. and Meth.* **A 382**, 419 (1996).
- [8] N. Harnew et al., *Nucl. Instr. and Meth.* **A 279**, 290 (1989);  
B. Foster et al., *Nucl. Phys. Proc. Suppl.* **B 32**, 181 (1993);  
B. Foster et al., *Nucl. Instr. and Meth.* **A 338**, 254 (1994).
- [9] ZEUS Collab., U. Holm (ed.), *The ZEUS Detector*, Status Report, (unpublished), DESY, 1993, available on <http://www-zeus.desy.de/bluebook/bluebook.html>.
- [10] A. Bamberger et al., *Nucl. Instr. and Meth.* **A 401**, 63 (1997).
- [11] J. Andruszków et al., Report DESY-92-066, DESY, 1992;  
ZEUS Collab., M. Derrick et al., *Z. Phys.* **C 63**, 391 (1994).
- [12] W.H. Smith et al., *Nucl. Instr. and Meth.* **A 355**, 278 (1995).
- [13] U. Bassler and G. Bernardi, *Nucl. Instr. and Meth.* **A 361**, 197 (1995).
- [14] R. Brun et al., GEANT3, Technical Report CERN-DD/EE/84-1, CERN, 1987.
- [15] A. Kwiatkowski, H. Spiesberger and H.-J. Möhring, *Comp. Phys. Comm.* **69**, 155 (1992). Also in *Proc. Workshop Physics at HERA*, 1991, DESY, Hamburg.
- [16] G. Ingelman, A. Edin and J. Rathsman, *Comp. Phys. Comm.* **101**, 108 (1997).
- [17] K. Charchula, G.A. Schuler and H. Spiesberger, *Comp. Phys. Comm.* **81**, 381 (1994).
- [18] Y. Azimov et al., *Phys. Lett.* **B 165**, 147 (1985);  
G. Gustafson and U. Petterson, *Nucl. Phys.* **B306**, 746 (1988);  
B. Andersson et al., *Z. Phys.* **C 43**, 625 (1989).

- [19] L. Lönnblad, *Comp. Phys. Comm.* **71**, 15 (1992).
- [20] T. Sjöstrand, *Comp. Phys. Comm.* **82**, 74 (1994).
- [21] ZEUS Collab., J. Breitweg et al., *Eur. Phys. J.* **C 6**, 239 (1999).
- [22] ZEUS Collab., J. Breitweg et al., *Eur. Phys. J.* **C 6**, 43 (1999).
- [23] H1 Collab., C. Adloff et al., *Z. Phys.* **C 76**, 613 (1997).
- [24] H. Jung, *Comp. Phys. Comm.* **86**, 147 (1995).
- [25] H.L. Lai et al., *Phys. Rev.* **D 51**, 4763 (1995).
- [26] ZEUS Collab., J. Breitweg et al., *Eur. Phys. J.* **C 1**, 109 (1998).
- [27] H. Abramowicz et al., *Phys. Lett.* **B 269**, 465 (1991).
- [28] H. Abramowicz, A. Caldwell and R. Sinkus, *Nucl. Instr. and Meth.* **A 365**, 508 (1995).
- [29] ZEUS Collab., J. Breitweg et al., *Eur. Phys. J.* **C 11**, 427 (1999).
- [30] F. Jacquet and A. Blondel, in *Proceedings of the Study for an ep Facility for Europe*, ed. U. Amaldi, p. 391. Hamburg, Germany, 1979. Also in preprint DESY 79/48.
- [31] S. Bentvelsen, J. Engelen and P. Kooijman, in *Proc. Workshop on Physics at HERA, Oct. 1991*, eds. W. Buchmüller and G. Ingelman, Vol. 1, p. 23. Hamburg, Germany, DESY, 1992;  
K.C. Höger, *Measurement of  $x$ ,  $y$  and  $Q^2$  in neutral current events*. Ibid, p.43.
- [32] N. Tuning, *Proton structure functions at HERA*. Ph.D. Thesis, University of Amsterdam, 2001, available on  
<http://www.nikhef.nl/pub/services/library.html>.
- [33] H.L. Lai et al., *Phys. Rev.* **D 55**, 1280 (1997).
- [34] A. Arbuzov et al., *Comp. Phys. Comm.* **94**, 128 (1996).
- [35] NMC Collab., M. Arneodo et al., *Nucl. Phys.* **B 483**, 3 (1997).
- [36] BCDMS Collab., A.C. Benvenuti et al., *Phys. Lett.* **B 223**, 485 (1989).
- [37] E665 Collab., M.R. Adams et al., *Phys. Rev.* **D 54**, 3006 (1996).
- [38] CTEQ Collab., H.L. Lai et al., *Eur. Phys. J.* **C 12**, 375 (2000).
- [39] A.D. Martin et al., *Eur. Phys. J.* **C 14**, 133 (2000).
- [40] NMC Collab., M. Arneodo et al., *Nucl. Phys.* **B 487**, 3 (1997).
- [41] CCFR Collab., E. Oltman et al., *Z. Phys.* **C 53**, 51 (1992).
- [42] R.S. Thorne and R.G. Roberts, *Phys. Rev.* **D 57**, 1998 (1998);  
R.S. Thorne and R.G. Roberts, *Phys. Lett.* **B 421**, 303 (1998).

[43] CCFR Collab., A.O. Bazarko et al., Z. Phys. **C65**, 189 (1995).



**Table 1:** *Results for the reduced cross section and the structure function  $F_2^{em}$ .  
The relative corrections in the last three columns are defined in Section 10.1.*

$Q^2$ (GeV <sup>2</sup> )	$x$	$y$	$N_{data}$	$N_{php}$	$\tilde{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$F_2^{em}$	$\Delta_{all}$ (%)	$\Delta_{F_2}$ (%)	$\Delta_{xF_3}$ (%)	$\Delta_{F_L}$ (%)
2.7	$6.32 \cdot 10^{-5}$	0.474	9506	769	0.832	1.7	4.7	0.869	-4.3	0.0	0.0	-4.3
2.7	$1.61 \cdot 10^{-4}$	0.186	21489	229	0.740	1.0	2.4	0.744	-0.6	0.0	0.0	-0.6
2.7	$4.00 \cdot 10^{-4}$	0.075	18716	47	0.649	1.1	3.9	0.650	-0.1	0.0	0.0	-0.1
2.7	$6.32 \cdot 10^{-4}$	0.047	8745	13	0.607	1.5	4.3	0.607	0.0	0.0	0.0	0.0
2.7	$2.00 \cdot 10^{-3}$	0.015	23981	6	0.477	0.9	4.2	0.477	0.0	0.0	0.0	0.0
3.5	$6.32 \cdot 10^{-5}$	0.614	5960	1422	1.076	2.7	12.7	1.177	-8.6	0.0	0.0	-8.6
3.5	$1.02 \cdot 10^{-4}$	0.380	6859	354	0.951	2.0	3.6	0.979	-2.9	0.0	0.0	-2.9
3.5	$1.61 \cdot 10^{-4}$	0.241	5818	62	0.882	2.0	2.5	0.891	-1.0	0.0	0.0	-1.0
3.5	$2.53 \cdot 10^{-4}$	0.153	6258	32	0.829	1.9	2.4	0.833	-0.4	0.0	0.0	-0.4
3.5	$4.00 \cdot 10^{-4}$	0.097	5676	0	0.787	1.9	2.7	0.788	-0.1	0.0	0.0	-0.2
3.5	$6.32 \cdot 10^{-4}$	0.061	5619	3	0.700	1.9	3.0	0.701	-0.1	0.0	0.0	-0.1
3.5	$2.00 \cdot 10^{-3}$	0.019	25800	11	0.554	0.9	2.5	0.554	0.0	0.0	0.0	0.0
3.5	$8.00 \cdot 10^{-3}$	0.005	17413	0	0.472	1.0	6.3	0.472	0.0	0.0	0.0	0.0
4.5	$1.02 \cdot 10^{-4}$	0.489	6886	824	1.125	2.0	5.8	1.189	-5.4	0.0	0.0	-5.4
4.5	$1.61 \cdot 10^{-4}$	0.310	5020	107	0.994	2.0	2.2	1.013	-1.9	0.0	0.0	-1.9
4.5	$2.53 \cdot 10^{-4}$	0.197	4476	10	0.923	2.0	2.6	0.929	-0.7	0.0	0.0	-0.7
4.5	$4.00 \cdot 10^{-4}$	0.125	3877	1	0.882	2.2	2.4	0.884	-0.3	0.0	0.0	-0.3
4.5	$6.32 \cdot 10^{-4}$	0.079	3708	5	0.803	2.2	2.0	0.804	-0.1	0.0	0.0	-0.1
6.5	$1.02 \cdot 10^{-4}$	0.706	6501	1382	1.210	2.4	10.2	1.392	-13.1	0.0	0.0	-13.1
6.5	$1.61 \cdot 10^{-4}$	0.448	9445	732	1.159	1.5	3.6	1.213	-4.4	0.0	0.0	-4.4
6.5	$2.53 \cdot 10^{-4}$	0.285	9279	159	1.078	1.5	1.9	1.094	-1.5	0.1	0.0	-1.6
6.5	$4.00 \cdot 10^{-4}$	0.180	7217	33	0.972	1.5	1.8	0.977	-0.6	0.0	0.0	-0.6
6.5	$6.32 \cdot 10^{-4}$	0.114	6435	7	0.898	1.6	3.1	0.900	-0.2	0.0	0.0	-0.2
6.5	$1.02 \cdot 10^{-3}$	0.071	6100	7	0.828	1.6	2.1	0.828	-0.1	0.0	0.0	-0.1
6.5	$1.61 \cdot 10^{-3}$	0.045	4958	11	0.740	1.8	2.5	0.740	0.0	0.0	0.0	0.0
6.5	$2.53 \cdot 10^{-3}$	0.028	9848	1	0.666	1.2	1.9	0.666	0.0	0.0	0.0	0.0
6.5	$5.00 \cdot 10^{-3}$	0.014	17517	0	0.576	0.9	4.1	0.576	0.0	0.0	0.0	0.0
6.5	$2.10 \cdot 10^{-2}$	0.003	11829	0	0.487	1.2	8.7	0.487	0.0	0.0	0.0	0.0
8.5	$1.61 \cdot 10^{-4}$	0.585	5783	1219	1.212	2.5	9.9	1.323	-8.4	0.0	0.0	-8.3
8.5	$2.53 \cdot 10^{-4}$	0.372	7175	321	1.188	1.6	2.7	1.223	-2.8	0.0	0.0	-2.9
8.5	$4.00 \cdot 10^{-4}$	0.236	6460	111	1.067	1.6	2.0	1.078	-1.0	0.0	0.0	-1.0

**Table 1** (continued): *Results for the reduced cross section and the structure function  $F_2^{em}$ .*

$Q^2$ (GeV <sup>2</sup> )	$x$	$y$	$N_{data}$	$N_{php}$	$\tilde{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$F_2^{em}$	$\Delta_{all}$ (%)	$\Delta_{F_2}$ (%)	$\Delta_{xF_3}$ (%)	$\Delta_{F_L}$ (%)
8.5	$6.32 \cdot 10^{-4}$	0.149	6028	24	0.973	1.6	2.8	0.977	-0.4	0.0	0.0	-0.4
8.5	$1.02 \cdot 10^{-3}$	0.092	5597	16	0.875	1.6	1.6	0.877	-0.1	0.0	0.0	-0.1
8.5	$1.61 \cdot 10^{-3}$	0.059	4719	8	0.813	1.8	1.6	0.813	0.0	0.0	0.0	-0.1
10	$1.61 \cdot 10^{-4}$	0.689	2222	570	1.230	4.2	12.8	1.400	-12.1	0.1	0.0	-12.2
10	$2.53 \cdot 10^{-4}$	0.438	4923	485	1.237	2.1	4.5	1.291	-4.2	0.0	0.0	-4.1
10	$4.00 \cdot 10^{-4}$	0.277	4588	125	1.099	1.9	2.3	1.115	-1.4	0.0	0.0	-1.4
10	$6.32 \cdot 10^{-4}$	0.175	4665	23	1.016	1.8	1.9	1.021	-0.5	0.0	0.0	-0.5
10	$1.02 \cdot 10^{-3}$	0.109	4575	1	0.934	1.8	1.9	0.935	-0.2	0.0	0.0	-0.2
10	$1.61 \cdot 10^{-3}$	0.069	3729	4	0.851	2.1	2.0	0.852	-0.1	0.0	0.0	-0.1
10	$2.53 \cdot 10^{-3}$	0.044	3879	5	0.761	2.0	2.4	0.761	0.0	0.0	0.0	0.0
10	$5.00 \cdot 10^{-3}$	0.022	11983	4	0.624	1.1	2.9	0.624	0.0	0.0	0.0	0.0
10	$2.10 \cdot 10^{-2}$	0.005	12719	0	0.503	1.1	6.8	0.503	0.0	0.0	0.0	0.0
12	$2.53 \cdot 10^{-4}$	0.526	3380	557	1.322	2.6	7.5	1.410	-6.3	0.0	0.0	-6.2
12	$4.00 \cdot 10^{-4}$	0.333	3427	169	1.191	2.3	2.7	1.217	-2.2	0.0	0.0	-2.1
12	$6.32 \cdot 10^{-4}$	0.211	3485	32	1.070	2.1	2.3	1.078	-0.7	0.0	0.0	-0.8
12	$1.02 \cdot 10^{-3}$	0.130	3402	4	0.983	2.0	1.9	0.985	-0.3	0.0	0.0	-0.3
12	$1.61 \cdot 10^{-3}$	0.083	2929	6	0.899	2.2	1.6	0.900	-0.1	0.0	0.0	-0.1
12	$2.53 \cdot 10^{-3}$	0.053	2915	1	0.793	2.1	1.9	0.794	0.0	0.0	0.0	0.0
15	$2.53 \cdot 10^{-4}$	0.657	2479	400	1.397	2.9	7.6	1.559	-10.4	0.1	0.0	-10.5
15	$4.00 \cdot 10^{-4}$	0.416	3486	255	1.258	2.3	3.7	1.303	-3.5	0.0	0.0	-3.5
15	$6.32 \cdot 10^{-4}$	0.263	3736	79	1.137	2.0	2.2	1.151	-1.2	0.0	0.0	-1.2
15	$1.02 \cdot 10^{-3}$	0.163	3779	15	1.055	1.9	1.9	1.059	-0.4	0.0	0.0	-0.4
15	$1.61 \cdot 10^{-3}$	0.103	3126	4	0.944	2.2	1.6	0.945	-0.1	0.0	0.0	-0.2
15	$2.53 \cdot 10^{-3}$	0.066	3182	0	0.836	2.1	1.6	0.837	0.0	0.0	0.0	-0.1
15	$5.00 \cdot 10^{-3}$	0.033	5672	3	0.706	1.5	1.5	0.706	0.0	0.0	0.0	0.0
15	$2.10 \cdot 10^{-2}$	0.008	13289	0	0.519	1.0	6.9	0.519	0.0	0.0	0.0	0.0
18	$5.00 \cdot 10^{-4}$	0.399	4653	424	1.284	1.9	4.1	1.325	-3.1	0.0	0.0	-3.1
18	$8.00 \cdot 10^{-4}$	0.249	3646	53	1.157	2.2	2.4	1.169	-1.0	0.0	0.0	-1.0
18	$1.30 \cdot 10^{-3}$	0.154	3571	8	1.038	2.0	2.2	1.041	-0.3	0.0	0.0	-0.3
18	$2.10 \cdot 10^{-3}$	0.095	2475	3	0.929	2.3	1.6	0.930	-0.1	0.0	0.0	-0.1
18	$3.20 \cdot 10^{-3}$	0.062	2421	5	0.851	2.4	1.8	0.851	0.0	0.0	0.0	0.0
18	$5.00 \cdot 10^{-3}$	0.040	4363	1	0.739	1.7	1.7	0.739	0.0	0.0	0.0	0.0
22	$5.00 \cdot 10^{-4}$	0.488	2430	184	1.357	2.5	4.0	1.425	-4.8	0.1	0.0	-4.8
22	$8.00 \cdot 10^{-4}$	0.305	2884	51	1.267	2.2	1.9	1.287	-1.6	0.0	0.0	-1.6

**Table 1** (continued): *Results for the reduced cross section and the structure function  $F_2^{em}$ .*

$Q^2$ (GeV <sup>2</sup> )	$x$	$y$	$N_{data}$	$N_{php}$	$\tilde{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$F_2^{em}$	$\Delta_{all}$ (%)	$\Delta_{F_2}$ (%)	$\Delta_{xF_3}$ (%)	$\Delta_{F_L}$ (%)
22	$1.30 \cdot 10^{-3}$	0.188	2830	15	1.065	2.3	2.3	1.071	-0.6	0.0	0.0	-0.5
22	$2.10 \cdot 10^{-3}$	0.116	2033	2	1.001	2.7	2.0	1.003	-0.2	0.0	0.0	-0.2
22	$3.20 \cdot 10^{-3}$	0.076	1986	5	0.905	2.6	1.7	0.905	-0.1	0.0	0.0	-0.1
22	$5.00 \cdot 10^{-3}$	0.049	2268	1	0.771	2.4	1.7	0.771	0.0	0.0	0.0	0.0
22	$8.00 \cdot 10^{-3}$	0.030	2161	0	0.656	2.4	1.7	0.656	0.0	0.0	0.0	0.0
22	$1.30 \cdot 10^{-2}$	0.019	3398	0	0.581	2.0	5.6	0.581	0.0	0.0	0.0	0.0
22	$3.20 \cdot 10^{-2}$	0.008	4541	0	0.512	1.8	6.9	0.512	0.0	0.0	0.0	0.0
27	$5.00 \cdot 10^{-4}$	0.599	1492	99	1.497	3.3	4.0	1.620	-7.6	0.0	0.0	-7.6
27	$8.00 \cdot 10^{-4}$	0.374	2460	58	1.294	2.5	2.2	1.325	-2.4	0.0	0.0	-2.4
27	$1.30 \cdot 10^{-3}$	0.230	2639	16	1.181	2.3	2.7	1.190	-0.8	0.0	0.0	-0.8
27	$2.10 \cdot 10^{-3}$	0.143	1910	4	1.095	2.8	1.7	1.098	-0.3	0.0	0.0	-0.3
27	$3.20 \cdot 10^{-3}$	0.094	1699	2	0.901	2.7	2.1	0.902	-0.1	0.0	0.0	-0.1
27	$5.00 \cdot 10^{-3}$	0.060	2016	0	0.804	2.5	2.5	0.804	0.0	0.0	0.0	0.0
27	$8.00 \cdot 10^{-3}$	0.037	1997	0	0.731	2.6	2.7	0.731	0.0	0.0	0.0	0.0
27	$1.30 \cdot 10^{-2}$	0.023	3210	0	0.634	2.0	2.9	0.634	0.0	0.0	0.0	0.0
35	$8.00 \cdot 10^{-4}$	0.485	23836	950	1.404	1.5	2.9	1.467	-4.3	0.1	0.0	-4.3
35	$1.30 \cdot 10^{-3}$	0.298	25024	204	1.225	1.4	1.8	1.241	-1.3	0.0	0.0	-1.3
35	$2.10 \cdot 10^{-3}$	0.185	17347	15	1.108	1.6	1.6	1.113	-0.5	0.0	0.0	-0.4
35	$3.20 \cdot 10^{-3}$	0.121	16475	5	0.961	1.7	1.6	0.963	-0.2	0.0	0.0	-0.2
35	$5.00 \cdot 10^{-3}$	0.078	19271	13	0.864	1.6	1.5	0.865	0.0	0.0	0.0	-0.1
35	$8.00 \cdot 10^{-3}$	0.049	18246	0	0.727	1.6	1.8	0.727	0.0	0.0	0.0	0.0
35	$1.30 \cdot 10^{-2}$	0.030	13171	0	0.646	1.9	2.2	0.646	0.0	0.0	0.0	0.0
35	$2.10 \cdot 10^{-2}$	0.018	14507	0	0.555	1.8	2.8	0.555	0.0	0.0	0.0	0.0
35	$3.20 \cdot 10^{-2}$	0.012	32311	0	0.496	1.1	7.6	0.496	0.0	0.0	0.0	0.0
45	$8.00 \cdot 10^{-4}$	0.624	13446	697	1.482	1.8	3.6	1.604	-7.6	0.0	0.0	-7.5
45	$1.30 \cdot 10^{-3}$	0.384	20011	245	1.297	1.3	2.1	1.327	-2.2	0.1	0.0	-2.3
45	$2.10 \cdot 10^{-3}$	0.238	14091	56	1.131	1.7	1.7	1.139	-0.7	0.0	0.0	-0.7
45	$3.20 \cdot 10^{-3}$	0.156	13613	5	0.998	1.5	1.5	1.001	-0.3	0.0	0.0	-0.3
45	$5.00 \cdot 10^{-3}$	0.100	15984	2	0.909	1.4	1.3	0.910	-0.1	0.0	0.0	-0.1
45	$8.00 \cdot 10^{-3}$	0.062	15340	0	0.777	1.4	1.5	0.777	0.0	0.0	0.0	0.0
45	$1.30 \cdot 10^{-2}$	0.038	10876	0	0.661	1.7	1.7	0.661	0.0	0.0	0.0	0.0
45	$2.10 \cdot 10^{-2}$	0.024	11920	0	0.587	1.7	2.1	0.587	0.0	0.0	0.0	0.0
60	$1.30 \cdot 10^{-3}$	0.512	18040	373	1.387	1.3	2.2	1.450	-4.3	0.0	0.0	-4.3
60	$2.10 \cdot 10^{-3}$	0.317	13355	143	1.213	1.5	1.8	1.230	-1.3	0.0	0.0	-1.4

**Table 1** (continued): *Results for the reduced cross section and the structure function  $F_2^{em}$ .*

$Q^2$ (GeV <sup>2</sup> )	$x$	$y$	$N_{data}$	$N_{php}$	$\tilde{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$F_2^{em}$	$\Delta_{all}$ (%)	$\Delta_{F_2}$ (%)	$\Delta_{xF_3}$ (%)	$\Delta_{F_L}$ (%)
60	$3.20 \cdot 10^{-3}$	0.208	13038	31	1.074	1.5	1.5	1.079	-0.5	0.1	0.0	-0.5
60	$5.00 \cdot 10^{-3}$	0.133	15083	6	0.900	1.4	1.5	0.902	-0.2	0.0	0.0	-0.2
60	$8.00 \cdot 10^{-3}$	0.083	14371	0	0.809	1.4	1.5	0.809	0.0	0.0	0.0	-0.1
60	$1.30 \cdot 10^{-2}$	0.051	10381	0	0.689	1.7	1.9	0.689	0.0	0.0	0.0	0.0
60	$2.10 \cdot 10^{-2}$	0.032	11570	0	0.598	1.6	2.4	0.598	0.0	0.1	0.0	0.0
60	$3.20 \cdot 10^{-2}$	0.021	8000	0	0.537	2.0	3.3	0.536	0.0	0.0	0.0	0.0
60	$5.00 \cdot 10^{-2}$	0.013	14942	0	0.512	1.5	6.8	0.512	0.0	0.0	0.0	0.0
70	$1.30 \cdot 10^{-3}$	0.597	9308	144	1.438	1.8	2.2	1.531	-6.1	0.1	0.0	-6.1
70	$2.10 \cdot 10^{-3}$	0.370	10323	142	1.238	1.7	1.9	1.262	-1.9	0.0	0.0	-1.9
70	$3.20 \cdot 10^{-3}$	0.243	9986	17	1.087	1.7	1.6	1.094	-0.6	0.1	0.0	-0.7
70	$5.00 \cdot 10^{-3}$	0.155	11939	2	0.984	1.5	1.5	0.986	-0.2	0.0	0.0	-0.2
70	$8.00 \cdot 10^{-3}$	0.097	11402	0	0.815	1.6	1.4	0.815	0.0	0.0	0.0	-0.1
70	$1.30 \cdot 10^{-2}$	0.060	8257	0	0.708	1.9	1.7	0.708	0.0	0.0	0.0	0.0
70	$2.10 \cdot 10^{-2}$	0.037	9567	0	0.620	1.8	1.6	0.620	0.0	0.0	0.0	0.0
70	$3.20 \cdot 10^{-2}$	0.024	6805	0	0.557	2.1	2.8	0.557	0.0	0.0	0.0	0.0
70	$5.00 \cdot 10^{-2}$	0.016	15253	0	0.500	1.6	6.2	0.500	0.0	0.0	0.0	0.0
90	$2.10 \cdot 10^{-3}$	0.475	6476	83	1.236	2.0	2.2	1.277	-3.2	0.1	0.0	-3.3
90	$3.20 \cdot 10^{-3}$	0.312	7362	10	1.168	1.9	1.7	1.182	-1.1	0.0	0.0	-1.2
90	$5.00 \cdot 10^{-3}$	0.200	8940	0	1.029	1.7	1.7	1.032	-0.4	0.1	0.0	-0.4
90	$8.00 \cdot 10^{-3}$	0.125	8642	2	0.896	1.8	1.5	0.897	-0.1	0.1	0.0	-0.1
90	$1.30 \cdot 10^{-2}$	0.077	6311	0	0.749	2.1	1.6	0.749	0.0	0.1	0.0	0.0
90	$2.10 \cdot 10^{-2}$	0.048	7083	0	0.622	1.9	1.9	0.621	0.0	0.1	0.0	0.0
90	$3.20 \cdot 10^{-2}$	0.031	4891	1	0.535	2.3	2.9	0.535	0.0	0.1	0.0	0.0
90	$5.00 \cdot 10^{-2}$	0.020	5982	0	0.484	2.1	6.3	0.484	0.0	0.1	0.0	0.0
90	$8.00 \cdot 10^{-2}$	0.012	7223	0	0.435	2.0	2.8	0.435	0.0	0.0	0.0	0.0
90	$1.80 \cdot 10^{-1}$	0.006	2981	0	0.340	3.1	5.3	0.339	0.1	0.1	0.0	0.0
120	$2.10 \cdot 10^{-3}$	0.634	3273	2	1.317	2.2	2.5	1.404	-6.2	0.1	0.0	-6.2
120	$3.20 \cdot 10^{-3}$	0.416	4812	13	1.173	1.9	2.0	1.198	-2.1	0.1	0.0	-2.2
120	$5.00 \cdot 10^{-3}$	0.266	6066	13	1.038	1.7	1.8	1.045	-0.7	0.1	0.0	-0.7
120	$8.00 \cdot 10^{-3}$	0.166	6203	0	0.908	1.8	1.4	0.910	-0.2	0.1	0.0	-0.2
120	$1.30 \cdot 10^{-2}$	0.102	4477	0	0.760	2.0	1.8	0.760	0.0	0.1	0.0	-0.1
120	$2.10 \cdot 10^{-2}$	0.063	5225	0	0.664	1.9	1.8	0.664	0.0	0.1	0.0	0.0
120	$3.20 \cdot 10^{-2}$	0.042	3712	0	0.579	2.3	2.2	0.579	0.1	0.1	0.0	0.0
120	$5.00 \cdot 10^{-2}$	0.027	4133	0	0.472	2.1	5.1	0.472	0.1	0.1	0.0	0.0

**Table 1** (continued): *Results for the reduced cross section and the structure function  $F_2^{em}$ .*

$Q^2$ (GeV <sup>2</sup> )	$x$	$y$	$N_{data}$	$N_{php}$	$\tilde{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$F_2^{em}$	$\Delta_{all}$ (%)	$\Delta_{F_2}$ (%)	$\Delta_{xF_3}$ (%)	$\Delta_{F_L}$ (%)
120	$8.00 \cdot 10^{-2}$	0.017	5409	0	0.437	1.9	4.7	0.436	0.0	0.1	0.0	0.0
120	$1.80 \cdot 10^{-1}$	0.007	2653	0	0.328	2.7	8.8	0.328	0.1	0.1	0.0	0.0
150	$3.20 \cdot 10^{-3}$	0.520	3655	7	1.194	2.1	2.3	1.238	-3.6	0.1	-0.1	-3.6
150	$5.00 \cdot 10^{-3}$	0.333	4977	0	1.037	1.9	1.8	1.049	-1.1	0.1	-0.1	-1.2
150	$8.00 \cdot 10^{-3}$	0.208	5111	0	0.887	1.8	1.6	0.890	-0.3	0.1	0.0	-0.4
150	$1.30 \cdot 10^{-2}$	0.128	3912	0	0.805	2.1	2.0	0.805	-0.1	0.1	0.0	-0.1
150	$2.10 \cdot 10^{-2}$	0.079	4382	0	0.661	2.0	1.9	0.660	0.0	0.1	0.0	0.0
150	$3.20 \cdot 10^{-2}$	0.052	3144	0	0.574	2.4	1.7	0.573	0.1	0.1	0.0	0.0
150	$5.00 \cdot 10^{-2}$	0.033	3622	0	0.515	2.2	2.3	0.515	0.1	0.1	0.0	0.0
150	$8.00 \cdot 10^{-2}$	0.021	4716	0	0.431	2.0	5.0	0.431	0.1	0.1	0.0	0.0
150	$1.80 \cdot 10^{-1}$	0.009	2580	0	0.326	2.7	6.4	0.326	0.1	0.1	0.0	0.0
200	$3.20 \cdot 10^{-3}$	0.693	1197	2	1.162	3.8	3.2	1.248	-6.9	0.2	-0.1	-6.9
200	$5.00 \cdot 10^{-3}$	0.443	3151	0	1.065	2.3	2.1	1.087	-2.1	0.2	-0.1	-2.2
200	$8.00 \cdot 10^{-3}$	0.277	3478	0	0.899	2.2	1.8	0.905	-0.6	0.2	-0.1	-0.7
200	$1.30 \cdot 10^{-2}$	0.171	3451	0	0.794	2.2	1.5	0.795	-0.1	0.1	-0.1	-0.2
200	$2.10 \cdot 10^{-2}$	0.106	2248	0	0.659	2.7	1.8	0.659	0.0	0.1	-0.1	-0.1
200	$3.20 \cdot 10^{-2}$	0.069	2142	0	0.570	2.8	1.9	0.570	0.1	0.1	-0.1	0.0
200	$5.00 \cdot 10^{-2}$	0.044	2393	0	0.508	2.8	2.4	0.508	0.1	0.1	0.0	0.0
200	$8.00 \cdot 10^{-2}$	0.028	3124	0	0.434	2.4	2.7	0.433	0.1	0.1	0.0	0.0
200	$1.80 \cdot 10^{-1}$	0.012	2161	0	0.340	2.9	3.7	0.339	0.1	0.1	0.0	0.0
250	$5.00 \cdot 10^{-3}$	0.554	1971	0	1.066	3.0	2.9	1.105	-3.6	0.3	-0.2	-3.7
250	$8.00 \cdot 10^{-3}$	0.346	2446	0	0.927	2.6	1.7	0.937	-1.1	0.2	-0.1	-1.1
250	$1.30 \cdot 10^{-2}$	0.213	2634	0	0.821	2.7	1.8	0.824	-0.3	0.2	-0.1	-0.3
250	$2.10 \cdot 10^{-2}$	0.132	1644	0	0.644	3.5	1.8	0.644	0.0	0.2	-0.1	-0.1
250	$3.20 \cdot 10^{-2}$	0.087	1646	0	0.612	3.4	2.3	0.612	0.1	0.2	-0.1	0.0
250	$5.00 \cdot 10^{-2}$	0.055	1838	0	0.517	3.2	1.8	0.516	0.1	0.2	-0.1	0.0
250	$8.00 \cdot 10^{-2}$	0.035	2365	0	0.445	2.8	5.1	0.445	0.1	0.2	-0.1	0.0
250	$1.80 \cdot 10^{-1}$	0.015	1729	0	0.341	3.2	5.6	0.340	0.1	0.2	0.0	0.0
350	$5.00 \cdot 10^{-3}$	0.776	810	0	1.103	4.4	3.5	1.196	-7.8	0.3	-0.3	-7.8
350	$8.00 \cdot 10^{-3}$	0.485	1924	2	0.988	2.9	2.1	1.011	-2.3	0.3	-0.3	-2.4
350	$1.30 \cdot 10^{-2}$	0.298	2037	0	0.824	2.9	1.7	0.829	-0.6	0.3	-0.2	-0.7
350	$2.10 \cdot 10^{-2}$	0.185	1355	0	0.679	3.6	1.9	0.680	-0.1	0.3	-0.2	-0.2
350	$3.20 \cdot 10^{-2}$	0.121	1329	0	0.639	3.6	2.0	0.639	0.0	0.3	-0.2	-0.1
350	$5.00 \cdot 10^{-2}$	0.078	1475	0	0.526	3.4	1.9	0.526	0.1	0.3	-0.1	0.0

**Table 1** (continued): *Results for the reduced cross section and the structure function  $F_2^{em}$ .*

$Q^2$ (GeV <sup>2</sup> )	$x$	$y$	$N_{data}$	$N_{php}$	$\tilde{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$F_2^{em}$	$\Delta_{all}$ (%)	$\Delta_{F_2}$ (%)	$\Delta_{xF_3}$ (%)	$\Delta_{F_L}$ (%)
350	$8.00 \cdot 10^{-2}$	0.049	1783	0	0.442	3.2	2.6	0.441	0.1	0.3	-0.1	0.0
350	$1.80 \cdot 10^{-1}$	0.022	1465	0	0.328	3.5	1.6	0.328	0.2	0.2	-0.1	0.0
450	$8.00 \cdot 10^{-3}$	0.624	1163	9	0.954	3.5	2.4	0.995	-4.2	0.4	-0.4	-4.2
450	$1.30 \cdot 10^{-2}$	0.384	1331	0	0.854	3.0	1.7	0.864	-1.2	0.4	-0.4	-1.2
450	$2.10 \cdot 10^{-2}$	0.238	932	0	0.702	3.6	1.6	0.704	-0.3	0.4	-0.3	-0.3
450	$3.20 \cdot 10^{-2}$	0.156	854	0	0.579	4.3	1.8	0.579	0.0	0.4	-0.3	-0.1
450	$5.00 \cdot 10^{-2}$	0.100	1009	0	0.511	3.4	1.5	0.511	0.1	0.4	-0.2	0.0
450	$8.00 \cdot 10^{-2}$	0.062	909	0	0.439	3.6	2.3	0.439	0.2	0.4	-0.2	0.0
450	$1.30 \cdot 10^{-1}$	0.038	830	0	0.365	3.8	2.3	0.365	0.2	0.4	-0.2	0.0
450	$2.50 \cdot 10^{-1}$	0.020	588	0	0.264	4.5	7.7	0.263	0.2	0.3	-0.1	0.0
650	$8.00 \cdot 10^{-3}$	0.901	529	0	0.926	4.6	3.2	1.023	-9.4	0.7	-0.8	-9.4
650	$1.30 \cdot 10^{-2}$	0.554	1056	2	0.827	3.3	1.9	0.850	-2.8	0.7	-0.8	-2.7
650	$2.10 \cdot 10^{-2}$	0.343	792	0	0.722	3.8	1.7	0.728	-0.8	0.7	-0.7	-0.8
650	$3.20 \cdot 10^{-2}$	0.225	712	0	0.603	4.0	1.9	0.604	-0.2	0.7	-0.6	-0.3
650	$5.00 \cdot 10^{-2}$	0.144	751	0	0.475	4.3	2.1	0.475	0.1	0.7	-0.5	-0.1
650	$8.00 \cdot 10^{-2}$	0.090	767	0	0.456	3.9	1.5	0.455	0.2	0.6	-0.4	0.0
650	$1.30 \cdot 10^{-1}$	0.055	641	0	0.357	4.2	3.2	0.356	0.3	0.6	-0.3	0.0
650	$2.50 \cdot 10^{-1}$	0.029	495	0	0.250	4.8	3.4	0.249	0.4	0.6	-0.2	0.0
650	$4.00 \cdot 10^{-1}$	0.018	132	0	0.152	9.5	14.5	0.151	0.3	0.4	-0.1	0.0
800	$1.30 \cdot 10^{-2}$	0.682	653	0	0.847	4.5	2.4	0.887	-4.6	0.9	-1.2	-4.3
800	$2.10 \cdot 10^{-2}$	0.422	436	0	0.665	7.5	1.6	0.675	-1.3	0.9	-1.0	-1.2
800	$3.20 \cdot 10^{-2}$	0.277	470	0	0.647	4.9	1.4	0.650	-0.4	0.9	-0.9	-0.4
800	$5.00 \cdot 10^{-2}$	0.177	449	0	0.451	5.0	2.3	0.451	0.0	0.9	-0.8	-0.1
800	$8.00 \cdot 10^{-2}$	0.111	473	0	0.420	5.8	2.6	0.419	0.2	0.8	-0.6	0.0
800	$1.30 \cdot 10^{-1}$	0.068	425	0	0.370	5.2	2.5	0.369	0.3	0.8	-0.5	0.0
800	$2.50 \cdot 10^{-1}$	0.035	337	0	0.260	5.9	1.8	0.259	0.4	0.7	-0.3	0.0
800	$4.00 \cdot 10^{-1}$	0.022	88	0	0.114	11.4	13.5	0.114	0.4	0.7	-0.2	0.0
1200	$1.40 \cdot 10^{-2}$	0.950	376	0	0.872	5.5	2.9	0.960	-9.2	1.6	-2.1	-8.7
1200	$2.10 \cdot 10^{-2}$	0.634	442	0	0.681	5.1	1.8	0.707	-3.7	1.6	-2.3	-3.0
1200	$3.20 \cdot 10^{-2}$	0.416	449	0	0.563	5.0	2.0	0.571	-1.4	1.6	-2.0	-1.0
1200	$5.00 \cdot 10^{-2}$	0.266	525	0	0.490	4.6	1.6	0.493	-0.4	1.5	-1.7	-0.3
1200	$8.00 \cdot 10^{-2}$	0.166	546	0	0.434	5.3	1.5	0.434	0.0	1.5	-1.4	-0.1
1200	$1.30 \cdot 10^{-1}$	0.102	460	0	0.336	5.8	3.1	0.335	0.3	1.4	-1.1	0.0
1200	$2.50 \cdot 10^{-1}$	0.053	392	0	0.254	5.4	2.0	0.253	0.6	1.3	-0.7	0.0

**Table 1** (continued): *Results for the reduced cross section and the structure function  $F_2^{em}$ .*

$Q^2$ (GeV <sup>2</sup> )	$x$	$y$	$N_{data}$	$N_{php}$	$\tilde{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$F_2^{em}$	$\Delta_{all}$ (%)	$\Delta_{F_2}$ (%)	$\Delta_{xF_3}$ (%)	$\Delta_{F_L}$ (%)
1200	$4.00 \cdot 10^{-1}$	0.033	176	0	0.149	8.1	10.3	0.148	0.7	1.2	-0.5	0.0
1200	$6.50 \cdot 10^{-1}$	0.020	9	0	0.021	35.6	25.1	0.021	0.7	1.0	-0.3	0.0
1500	$2.10 \cdot 10^{-2}$	0.792	206	0	0.666	7.9	6.2	0.710	-6.1	2.2	-3.3	-5.1
1500	$3.20 \cdot 10^{-2}$	0.520	260	0	0.540	10.3	2.0	0.554	-2.5	2.2	-3.1	-1.6
1500	$5.00 \cdot 10^{-2}$	0.333	320	0	0.518	5.8	1.8	0.523	-1.0	2.1	-2.6	-0.5
1500	$8.00 \cdot 10^{-2}$	0.208	338	0	0.476	5.7	2.6	0.477	-0.2	2.0	-2.1	-0.1
1500	$1.30 \cdot 10^{-1}$	0.128	216	0	0.301	11.8	1.9	0.300	0.3	1.9	-1.6	0.0
1500	$1.80 \cdot 10^{-1}$	0.092	202	0	0.313	7.3	5.9	0.311	0.5	1.8	-1.3	0.0
1500	$2.50 \cdot 10^{-1}$	0.067	146	0	0.270	8.6	3.0	0.268	0.7	1.7	-1.0	0.0
1500	$4.00 \cdot 10^{-1}$	0.042	69	0	0.146	12.6	13.7	0.145	0.9	1.6	-0.7	0.0
1500	$6.50 \cdot 10^{-1}$	0.026	11	0	0.012	30.9	19.0	0.012	0.9	1.4	-0.4	0.0
2000	$3.20 \cdot 10^{-2}$	0.693	156	0	0.586	8.3	3.4	0.617	-5.1	3.2	-5.2	-3.1
2000	$5.00 \cdot 10^{-2}$	0.443	195	0	0.476	7.4	2.0	0.487	-2.3	3.2	-4.6	-0.9
2000	$8.00 \cdot 10^{-2}$	0.277	213	0	0.444	7.1	2.0	0.448	-0.9	3.0	-3.7	-0.2
2000	$1.30 \cdot 10^{-1}$	0.171	154	0	0.340	8.3	3.9	0.340	0.0	2.9	-2.8	-0.1
2000	$1.80 \cdot 10^{-1}$	0.123	131	0	0.282	9.1	2.6	0.280	0.4	2.7	-2.3	0.0
2000	$2.50 \cdot 10^{-1}$	0.089	100	0	0.234	10.4	5.3	0.232	0.7	2.5	-1.8	0.0
2000	$4.00 \cdot 10^{-1}$	0.055	58	0	0.170	13.8	10.1	0.169	1.1	2.3	-1.2	0.0
3000	$5.00 \cdot 10^{-2}$	0.665	140	0	0.542	8.7	2.1	0.578	-6.2	5.5	-9.4	-2.3
3000	$8.00 \cdot 10^{-2}$	0.416	144	0	0.438	8.5	2.2	0.452	-3.2	5.2	-7.9	-0.6
3000	$1.30 \cdot 10^{-1}$	0.256	110	0	0.325	13.9	4.4	0.329	-1.1	4.9	-5.9	-0.1
3000	$1.80 \cdot 10^{-1}$	0.185	76	0	0.243	11.7	3.8	0.243	-0.2	4.6	-4.8	-0.1
3000	$2.50 \cdot 10^{-1}$	0.133	62	0	0.193	17.7	4.2	0.192	0.6	4.4	-3.7	0.0
3000	$4.00 \cdot 10^{-1}$	0.083	22	0	0.089	21.7	9.1	0.088	1.4	3.9	-2.5	0.0
3000	$6.50 \cdot 10^{-1}$	0.051	9	0	0.016	33.9	15.3	0.016	2.0	3.5	-1.5	0.0
5000	$8.00 \cdot 10^{-2}$	0.693	142	2	0.376	9.0	2.7	0.422	-10.9	9.8	-18.8	-1.9
5000	$1.30 \cdot 10^{-1}$	0.426	76	0	0.284	11.7	2.0	0.302	-6.1	9.2	-14.8	-0.4
5000	$1.80 \cdot 10^{-1}$	0.308	81	0	0.278	11.3	5.2	0.288	-3.3	8.7	-11.9	-0.2
5000	$2.50 \cdot 10^{-1}$	0.222	60	0	0.223	13.2	3.5	0.226	-1.2	8.1	-9.2	-0.1
5000	$4.00 \cdot 10^{-1}$	0.139	31	0	0.126	18.3	5.4	0.125	1.2	7.2	-6.0	0.0
8000	$1.30 \cdot 10^{-1}$	0.682	48	0	0.241	14.5	4.2	0.293	-17.8	15.1	-31.5	-1.3
8000	$1.80 \cdot 10^{-1}$	0.493	43	0	0.272	15.4	5.6	0.311	-12.4	14.2	-26.1	-0.5
8000	$2.50 \cdot 10^{-1}$	0.355	31	0	0.199	18.1	10.8	0.214	-7.2	13.2	-20.2	-0.2
8000	$4.00 \cdot 10^{-1}$	0.222	18	0	0.119	23.8	6.8	0.121	-1.4	11.7	-13.1	0.0

**Table 1** (continued): *Results for the reduced cross section and the structure function  $F_2^{em}$ .*

$Q^2$ (GeV <sup>2</sup> )	$x$	$y$	$N_{data}$	$N_{ph\bar{p}}$	$\tilde{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$F_2^{em}$	$\Delta_{all}$ (%)	$\Delta_{F_2}$ (%)	$\Delta_{xF_3}$ (%)	$\Delta_{F_L}$ (%)
8000	$6.50 \cdot 10^{-1}$	0.136	11	0	0.036	30.6	14.2	0.035	2.8	10.6	-7.9	0.0
12000	$1.80 \cdot 10^{-1}$	0.739	25	0	0.238	20.1	3.7	0.330	-27.9	20.1	-46.7	-1.2
12000	$2.50 \cdot 10^{-1}$	0.532	15	0	0.172	25.9	4.1	0.214	-19.8	18.6	-38.0	-0.4
12000	$4.00 \cdot 10^{-1}$	0.333	7	0	0.084	38.0	3.3	0.092	-8.2	16.6	-24.7	-0.1
20000	$2.50 \cdot 10^{-1}$	0.887	8	0	0.161	35.4	5.2	0.293	-44.9	26.1	-69.5	-1.4
20000	$4.00 \cdot 10^{-1}$	0.554	4	0	0.080	$^{+79}_{-48}$	13.9	0.112	-28.9	23.2	-51.8	-0.3
30000	$4.00 \cdot 10^{-1}$	0.831	1	0	0.039	$^{+230}_{-83}$	6.8	0.086	-53.9	28.2	-81.4	-0.7



**Table 2:** *Relative uncertainties in the reduced cross section. The systematic uncertainties, denoted by the {}, are explained in Section 10.2. The overall normalisation uncertainty of 2% is not included, neither is the additional uncertainty of 1% at low  $Q^2$ .*

$Q^2$ (GeV <sup>2</sup> )	$x$	$\bar{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$\delta_{unc}$ (%)	$\delta_{\{1\}}$ (%)	$\delta_{\{2\}}$ (%)	$\delta_{\{3\}}$ (%)	$\delta_{\{4\}}$ (%)	$\delta_{\{5\}}$ (%)	$\delta_{\{6\}}$ (%)	$\delta_{\{7\}}$ (%)	$\delta_{\{8\}}$ (%)	$\delta_{\{9\}}$ (%)	$\delta_{\{10\}}$ (%)
2.7	$6.32 \cdot 10^{-5}$	0.832	1.7	4.7	2.0	1.9	-0.1	0.0	0.2	0.1	0.2	1.4	1.9	2.9	0.3
2.7	$1.61 \cdot 10^{-4}$	0.740	1.0	2.4	1.8	1.4	0.3	0.0	-0.2	0.1	0.2	-0.3	0.1	0.4	-0.2
2.7	$4.00 \cdot 10^{-4}$	0.649	1.1	3.9	3.6	1.2	0.3	0.0	-0.3	0.1	0.4	-0.4	0.7	0.1	0.0
2.7	$6.32 \cdot 10^{-4}$	0.607	1.5	4.3	3.4	1.1	0.3	0.0	-0.5	0.6	-0.2	0.1	2.3	0.0	-0.1
2.7	$2.00 \cdot 10^{-3}$	0.477	0.9	4.2	2.7	1.1	0.1	0.0	-0.2	0.5	-0.1	-0.1	0.8	0.0	2.8
3.5	$6.32 \cdot 10^{-5}$	1.076	2.7	12.7	3.9	2.6	0.6	0.0	0.8	-0.1	0.4	2.6	4.3	10.6	0.1
3.5	$1.02 \cdot 10^{-4}$	0.951	2.0	3.6	2.0	1.7	0.3	0.0	0.7	0.1	0.1	0.8	0.8	1.9	0.1
3.5	$1.61 \cdot 10^{-4}$	0.882	2.0	2.5	1.9	1.4	0.1	0.0	0.3	-0.1	0.3	0.3	0.1	0.4	0.0
3.5	$2.53 \cdot 10^{-4}$	0.829	1.9	2.4	1.7	1.3	-0.4	0.0	-0.5	0.1	0.4	-0.6	-0.2	0.2	-0.2
3.5	$4.00 \cdot 10^{-4}$	0.787	1.9	2.7	2.1	1.2	-0.3	0.0	-0.4	-0.3	0.3	-0.5	0.8	0.0	0.3
3.5	$6.32 \cdot 10^{-4}$	0.700	1.9	3.0	2.5	1.1	0.2	0.0	0.4	0.3	0.3	-0.1	1.0	0.0	0.1
3.5	$2.00 \cdot 10^{-3}$	0.554	0.9	2.5	1.4	1.1	-0.1	0.0	-0.3	0.5	-0.1	0.0	0.8	0.0	1.5
3.5	$8.00 \cdot 10^{-3}$	0.472	1.0	6.3	1.6	1.1	-0.2	0.0	-0.5	0.7	-0.1	-0.1	-0.2	0.0	5.9
4.5	$1.02 \cdot 10^{-4}$	1.125	2.0	5.8	1.3	2.0	-0.4	0.0	0.3	-0.1	0.2	1.7	1.9	4.6	-0.1
4.5	$1.61 \cdot 10^{-4}$	0.994	2.0	2.2	0.7	1.6	0.6	0.0	0.3	0.1	0.2	0.3	0.7	0.7	0.0
4.5	$2.53 \cdot 10^{-4}$	0.923	2.0	2.6	1.9	1.3	0.0	0.0	-0.5	0.1	0.2	-0.3	1.1	0.1	0.0
4.5	$4.00 \cdot 10^{-4}$	0.882	2.2	2.4	1.9	1.2	-0.4	0.0	-0.4	-0.1	-0.2	-0.6	0.3	0.0	-0.3
4.5	$6.32 \cdot 10^{-4}$	0.803	2.2	2.0	1.4	1.2	-0.4	0.0	-0.1	0.2	0.3	-0.2	0.7	0.0	0.2
6.5	$1.02 \cdot 10^{-4}$	1.210	2.4	10.2	1.0	2.5	0.3	0.0	0.3	-0.2	0.5	2.5	2.4	9.2	0.2
6.5	$1.61 \cdot 10^{-4}$	1.159	1.5	3.6	0.4	1.8	0.0	0.0	0.6	0.1	0.1	0.6	0.9	2.8	0.0
6.5	$2.53 \cdot 10^{-4}$	1.078	1.5	1.9	0.5	1.5	0.4	0.0	0.5	0.1	0.3	0.3	0.5	0.6	0.0
6.5	$4.00 \cdot 10^{-4}$	0.972	1.5	1.8	0.9	1.3	-0.1	0.0	-0.4	-0.1	0.3	-0.6	-0.2	0.2	0.0
6.5	$6.32 \cdot 10^{-4}$	0.898	1.6	3.1	2.7	1.2	-0.2	0.0	-0.2	0.2	0.3	-0.4	0.4	0.0	0.0
6.5	$1.02 \cdot 10^{-3}$	0.828	1.6	2.1	1.6	1.1	0.3	0.0	-0.3	0.3	0.2	0.1	0.6	0.0	-0.1
6.5	$1.61 \cdot 10^{-3}$	0.740	1.8	2.5	2.0	1.1	-0.7	0.0	-0.4	-0.5	-0.3	-0.1	0.4	0.0	0.6
6.5	$2.53 \cdot 10^{-3}$	0.666	1.2	1.9	1.1	1.1	0.2	0.0	0.3	0.6	0.0	0.0	0.6	0.0	0.5
6.5	$5.00 \cdot 10^{-3}$	0.576	0.9	4.1	0.9	1.1	0.2	0.0	-0.3	0.4	0.0	0.1	0.0	0.0	3.9
6.5	$2.10 \cdot 10^{-2}$	0.487	1.2	8.7	1.9	1.1	-0.2	0.0	-0.7	0.8	-0.4	0.0	-0.5	0.0	8.3
8.5	$1.61 \cdot 10^{-4}$	1.212	2.5	9.9	1.7	2.4	0.6	0.0	-1.0	0.2	0.4	1.8	1.8	9.1	0.0
8.5	$2.53 \cdot 10^{-4}$	1.188	1.6	2.7	0.9	1.6	0.6	0.0	0.6	-0.1	0.2	0.4	0.2	1.6	0.2
8.5	$4.00 \cdot 10^{-4}$	1.067	1.6	2.0	0.9	1.4	0.6	0.0	-0.4	0.1	0.2	-0.4	0.1	0.6	-0.2
8.5	$6.32 \cdot 10^{-4}$	0.973	1.6	2.8	1.9	1.2	1.4	0.0	0.3	-0.1	0.4	-0.3	-0.2	0.1	0.3
8.5	$1.02 \cdot 10^{-3}$	0.875	1.6	1.6	0.8	1.2	-0.4	0.0	-0.4	-0.1	0.2	-0.3	0.0	0.1	-0.2
8.5	$1.61 \cdot 10^{-3}$	0.813	1.8	1.6	1.0	1.1	0.3	0.0	-0.1	0.3	0.0	-0.1	0.5	0.1	-0.3
10.0	$1.61 \cdot 10^{-4}$	1.230	4.2	12.8	1.4	2.7	-0.7	0.0	-0.6	-0.1	0.5	3.1	1.3	11.9	0.1
10.0	$2.53 \cdot 10^{-4}$	1.237	2.1	4.5	1.3	1.9	0.3	0.0	-0.3	-0.2	-0.1	0.7	-0.1	3.8	0.1
10.0	$4.00 \cdot 10^{-4}$	1.099	1.9	2.3	1.1	1.5	0.8	0.0	-0.2	0.1	0.3	-0.5	0.2	1.0	0.0
10.0	$6.32 \cdot 10^{-4}$	1.016	1.8	1.9	1.2	1.3	0.4	0.0	-0.1	-0.2	0.4	-0.6	-0.1	0.2	-0.1
10.0	$1.02 \cdot 10^{-3}$	0.934	1.8	1.9	1.3	1.2	0.2	0.0	-0.4	-0.2	0.2	-0.4	-0.2	0.0	0.0
10.0	$1.61 \cdot 10^{-3}$	0.851	2.1	2.0	1.2	1.1	1.1	0.0	0.2	-0.3	0.1	0.1	0.0	0.0	-0.1
10.0	$2.53 \cdot 10^{-3}$	0.761	2.0	2.4	1.8	1.1	0.9	0.0	-0.2	0.4	-0.2	-0.1	0.4	0.0	-0.4
10.0	$5.00 \cdot 10^{-3}$	0.624	1.1	2.9	0.8	1.1	0.8	0.0	-0.2	0.6	-0.1	0.0	0.1	0.0	2.4

**Table 2** (continued): *Relative uncertainties in the reduced cross section.*

$Q^2$ (GeV <sup>2</sup> )	$x$	$\tilde{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$\delta_{unc}$ (%)	$\delta_{\{1\}}$ (%)	$\delta_{\{2\}}$ (%)	$\delta_{\{3\}}$ (%)	$\delta_{\{4\}}$ (%)	$\delta_{\{5\}}$ (%)	$\delta_{\{6\}}$ (%)	$\delta_{\{7\}}$ (%)	$\delta_{\{8\}}$ (%)	$\delta_{\{9\}}$ (%)	$\delta_{\{10\}}$ (%)
10.0	$2.10 \cdot 10^{-2}$	0.503	1.1	6.8	1.3	1.0	0.7	0.0	-0.7	0.9	-0.2	0.1	-0.2	0.0	6.5
12.0	$2.53 \cdot 10^{-4}$	1.322	2.6	7.5	1.0	2.2	1.3	0.0	-1.0	0.2	0.3	1.0	0.5	6.8	0.2
12.0	$4.00 \cdot 10^{-4}$	1.191	2.3	2.7	0.9	1.6	0.6	0.0	0.2	-0.2	-0.1	0.1	0.3	1.9	0.0
12.0	$6.32 \cdot 10^{-4}$	1.070	2.1	2.3	1.6	1.3	0.3	0.0	-0.1	-0.2	0.2	-0.6	0.5	0.3	0.1
12.0	$1.02 \cdot 10^{-3}$	0.983	2.0	1.9	1.1	1.2	0.8	0.0	-0.2	0.2	0.4	-0.5	0.3	0.0	-0.1
12.0	$1.61 \cdot 10^{-3}$	0.899	2.2	1.6	0.7	1.1	0.8	0.0	-0.2	0.1	0.2	-0.1	0.1	0.1	0.1
12.0	$2.53 \cdot 10^{-3}$	0.793	2.1	1.9	1.0	1.1	0.6	0.0	0.4	0.3	-0.1	0.0	0.1	0.0	0.9
15.0	$2.53 \cdot 10^{-4}$	1.397	2.9	7.6	1.5	2.3	0.7	0.0	0.5	0.2	0.2	2.0	0.7	6.7	-0.1
15.0	$4.00 \cdot 10^{-4}$	1.258	2.3	3.7	1.5	1.8	0.4	0.0	-0.3	-0.2	0.3	0.1	0.8	2.7	0.0
15.0	$6.32 \cdot 10^{-4}$	1.137	2.0	2.2	0.9	1.4	1.0	0.0	-0.2	-0.1	0.3	-0.2	0.3	0.8	-0.2
15.0	$1.02 \cdot 10^{-3}$	1.055	1.9	1.9	1.1	1.2	0.3	0.0	-0.2	-0.3	0.3	-0.6	0.2	0.1	0.1
15.0	$1.61 \cdot 10^{-3}$	0.944	2.2	1.6	0.7	1.2	0.6	0.0	-0.5	0.1	0.0	-0.2	0.1	0.0	-0.1
15.0	$2.53 \cdot 10^{-3}$	0.836	2.1	1.6	0.9	1.1	0.6	0.0	-0.3	0.3	-0.1	-0.1	0.1	0.0	-0.2
15.0	$5.00 \cdot 10^{-3}$	0.706	1.5	1.5	0.8	1.1	0.3	0.0	-0.1	0.5	-0.1	0.0	0.2	0.0	0.1
15.0	$2.10 \cdot 10^{-2}$	0.519	1.0	6.9	1.0	1.0	0.7	0.0	-0.6	0.5	-0.2	0.1	-0.2	0.0	6.6
18.0	$5.00 \cdot 10^{-4}$	1.284	1.9	4.1	0.7	1.9	0.4	0.0	-0.5	0.1	0.3	0.4	0.2	3.5	0.1
18.0	$8.00 \cdot 10^{-4}$	1.157	2.2	2.4	0.9	1.4	1.4	0.0	-0.1	-0.1	0.3	-0.6	0.1	0.5	0.3
18.0	$1.30 \cdot 10^{-3}$	1.038	2.0	2.2	1.5	1.2	0.8	0.0	-0.3	-0.1	0.4	-0.4	0.3	0.1	0.1
18.0	$2.10 \cdot 10^{-3}$	0.929	2.3	1.6	0.9	1.1	0.2	0.0	0.0	-0.2	-0.2	-0.2	0.4	0.0	-0.5
18.0	$3.20 \cdot 10^{-3}$	0.851	2.4	1.8	1.0	1.1	0.9	0.0	-0.5	0.2	0.2	0.1	0.2	0.1	0.2
18.0	$5.00 \cdot 10^{-3}$	0.739	1.7	1.7	0.6	1.1	0.9	0.0	-0.2	0.4	-0.2	0.0	-0.1	0.0	0.6
22.0	$5.00 \cdot 10^{-4}$	1.357	2.5	4.0	1.2	2.0	0.5	0.0	-1.0	0.1	0.2	0.6	0.7	2.8	0.0
22.0	$8.00 \cdot 10^{-4}$	1.267	2.2	1.9	0.6	1.5	-0.1	0.0	0.3	-0.1	0.3	-0.1	0.3	0.6	-0.5
22.0	$1.30 \cdot 10^{-3}$	1.065	2.3	2.3	1.4	1.3	1.0	0.0	-0.1	-0.2	0.4	-0.5	0.0	0.2	0.1
22.0	$2.10 \cdot 10^{-3}$	1.001	2.7	2.0	0.8	1.2	0.8	0.0	-1.0	0.2	-0.3	-0.2	0.3	0.0	-0.1
22.0	$3.20 \cdot 10^{-3}$	0.905	2.6	1.7	1.2	1.1	0.3	0.0	0.1	-0.4	0.1	-0.1	0.3	0.1	0.1
22.0	$5.00 \cdot 10^{-3}$	0.771	2.4	1.7	0.9	1.1	0.4	0.0	-0.3	0.3	-0.2	-0.1	0.2	0.0	-0.7
22.0	$8.00 \cdot 10^{-3}$	0.656	2.4	1.7	0.9	1.1	0.4	0.0	-0.7	0.5	-0.3	0.0	0.3	0.0	0.1
22.0	$1.30 \cdot 10^{-2}$	0.581	2.0	5.6	1.8	1.0	0.9	0.0	-0.3	0.4	0.1	-0.1	0.0	0.0	5.1
22.0	$3.20 \cdot 10^{-2}$	0.512	1.8	6.9	1.6	1.0	0.9	0.0	-0.7	1.4	-0.3	0.1	-0.3	0.0	6.4
27.0	$5.00 \cdot 10^{-4}$	1.497	3.3	4.0	1.5	2.1	0.7	0.0	0.1	0.2	0.2	1.3	0.9	2.5	0.3
27.0	$8.00 \cdot 10^{-4}$	1.294	2.5	2.2	0.8	1.7	0.4	0.0	0.1	0.1	0.3	0.2	0.4	0.9	0.0
27.0	$1.30 \cdot 10^{-3}$	1.181	2.3	2.7	1.8	1.4	1.1	0.0	-0.2	0.1	0.2	-0.6	0.1	0.2	0.0
27.0	$2.10 \cdot 10^{-3}$	1.095	2.8	1.7	1.0	1.2	0.5	0.0	0.2	-0.1	0.3	-0.2	0.0	0.1	0.0
27.0	$3.20 \cdot 10^{-3}$	0.901	2.7	2.1	1.5	1.2	0.8	0.0	0.1	0.2	-0.2	0.0	0.5	0.1	0.0
27.0	$5.00 \cdot 10^{-3}$	0.804	2.5	2.5	1.5	1.1	1.0	0.0	-1.1	0.2	-0.5	-0.1	0.3	0.0	-0.2
27.0	$8.00 \cdot 10^{-3}$	0.731	2.6	2.7	1.3	1.1	1.2	0.0	-0.4	0.7	-0.2	0.1	0.1	0.0	1.4
27.0	$1.30 \cdot 10^{-2}$	0.634	2.0	2.9	1.4	1.0	0.6	0.0	-0.4	0.3	0.0	0.1	-0.1	0.0	2.2
35.0	$8.00 \cdot 10^{-4}$	1.404	1.5	2.9	0.7	1.9	0.4	0.0	-1.0	0.0	0.0	0.3	1.1	1.4	0.0
35.0	$1.30 \cdot 10^{-3}$	1.225	1.4	1.8	0.3	1.5	0.5	0.0	-0.3	-0.1	0.4	-0.5	0.3	0.3	0.1
35.0	$2.10 \cdot 10^{-3}$	1.108	1.6	1.6	0.4	1.3	0.6	0.0	-0.5	-0.1	0.3	-0.4	0.1	0.0	-0.1
35.0	$3.20 \cdot 10^{-3}$	0.961	1.7	1.6	0.7	1.2	0.6	0.0	0.3	0.1	0.1	-0.1	-0.4	0.0	-0.2
35.0	$5.00 \cdot 10^{-3}$	0.864	1.6	1.5	0.4	1.1	0.6	0.0	-0.6	0.2	0.1	0.1	-0.1	0.0	-0.1
35.0	$8.00 \cdot 10^{-3}$	0.727	1.6	1.8	0.7	1.1	0.7	0.0	-0.4	0.5	-0.4	0.0	0.1	0.0	-0.6
35.0	$1.30 \cdot 10^{-2}$	0.646	1.9	2.2	0.9	1.1	0.5	0.0	-0.3	0.9	-0.1	-0.1	0.0	0.0	1.4
35.0	$2.10 \cdot 10^{-2}$	0.555	1.8	2.8	1.1	1.0	1.0	0.0	-0.5	-0.3	-0.2	0.2	-0.2	0.0	2.0
35.0	$3.20 \cdot 10^{-2}$	0.496	1.1	7.6	1.0	1.0	0.9	0.0	-1.2	0.9	-0.2	0.1	-0.2	0.0	7.2
45.0	$8.00 \cdot 10^{-4}$	1.482	1.8	3.6	1.4	2.0	0.4	0.0	0.3	-0.1	0.3	1.6	0.1	1.9	0.0

**Table 2** (continued): *Relative uncertainties in the reduced cross section.*

$Q^2$ (GeV <sup>2</sup> )	$x$	$\bar{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$\delta_{unc}$ (%)	$\delta_{\{1\}}$ (%)	$\delta_{\{2\}}$ (%)	$\delta_{\{3\}}$ (%)	$\delta_{\{4\}}$ (%)	$\delta_{\{5\}}$ (%)	$\delta_{\{6\}}$ (%)	$\delta_{\{7\}}$ (%)	$\delta_{\{8\}}$ (%)	$\delta_{\{9\}}$ (%)	$\delta_{\{10\}}$ (%)
45.0	$1.30 \cdot 10^{-3}$	1.297	1.3	2.1	0.3	1.6	0.5	0.0	-0.7	0.0	0.3	-0.8	0.2	0.4	0.0
45.0	$2.10 \cdot 10^{-3}$	1.131	1.7	1.7	0.4	1.4	0.5	0.0	-0.2	0.1	0.6	-0.3	-0.1	0.1	0.1
45.0	$3.20 \cdot 10^{-3}$	0.998	1.5	1.5	0.5	1.2	0.6	0.0	-0.2	0.2	0.1	-0.2	0.0	0.0	-0.2
45.0	$5.00 \cdot 10^{-3}$	0.909	1.4	1.3	0.4	1.2	0.2	0.0	-0.2	0.2	0.1	-0.2	-0.2	0.0	0.1
45.0	$8.00 \cdot 10^{-3}$	0.777	1.4	1.5	0.4	1.1	0.5	0.0	-0.5	-0.4	-0.3	-0.1	0.3	0.0	0.1
45.0	$1.30 \cdot 10^{-2}$	0.661	1.7	1.7	0.8	1.1	0.2	0.0	-0.8	0.6	-0.2	-0.1	-0.1	0.0	-0.1
45.0	$2.10 \cdot 10^{-2}$	0.587	1.7	2.1	0.3	1.0	0.4	0.0	-0.6	0.3	0.0	0.1	-0.3	0.0	1.6
60.0	$1.30 \cdot 10^{-3}$	1.387	1.3	2.2	0.6	1.8	0.5	-0.1	-0.4	0.1	0.1	-0.1	0.4	0.7	0.0
60.0	$2.10 \cdot 10^{-3}$	1.213	1.5	1.8	0.5	1.5	0.4	0.0	-0.2	-0.2	0.4	-0.4	0.4	0.4	-0.1
60.0	$3.20 \cdot 10^{-3}$	1.074	1.5	1.5	0.4	1.3	0.4	0.0	0.2	-0.1	0.4	-0.3	-0.2	0.1	-0.1
60.0	$5.00 \cdot 10^{-3}$	0.900	1.4	1.5	0.5	1.2	0.4	0.0	0.4	0.2	0.3	-0.1	0.2	0.0	0.1
60.0	$8.00 \cdot 10^{-3}$	0.809	1.4	1.5	0.7	1.1	0.5	0.0	-0.6	0.2	-0.3	0.1	0.2	0.0	0.1
60.0	$1.30 \cdot 10^{-2}$	0.689	1.7	1.9	0.8	1.1	0.7	0.0	-0.6	0.7	-0.3	0.1	0.2	0.0	-0.5
60.0	$2.10 \cdot 10^{-2}$	0.598	1.6	2.4	1.1	1.1	0.6	0.0	-0.7	0.2	-0.1	0.1	0.0	0.0	1.5
60.0	$3.20 \cdot 10^{-2}$	0.537	2.0	3.3	1.3	1.0	0.5	0.0	-0.6	0.7	0.0	0.2	-0.2	0.0	2.7
60.0	$5.00 \cdot 10^{-2}$	0.512	1.5	6.8	1.9	1.0	0.0	0.0	-0.8	0.9	-0.3	-0.1	-0.1	0.0	6.3
70.0	$1.30 \cdot 10^{-3}$	1.438	1.8	2.2	0.6	1.9	0.3	-0.3	-0.5	0.1	0.1	0.3	-0.3	0.5	0.0
70.0	$2.10 \cdot 10^{-3}$	1.238	1.7	1.9	0.3	1.6	0.4	-0.1	0.3	0.1	0.4	-0.3	0.4	0.5	0.1
70.0	$3.20 \cdot 10^{-3}$	1.087	1.7	1.6	0.5	1.4	0.5	0.0	-0.2	-0.1	0.3	-0.3	0.0	0.1	-0.1
70.0	$5.00 \cdot 10^{-3}$	0.984	1.5	1.5	0.4	1.2	0.5	0.0	-0.3	0.2	0.2	-0.1	-0.2	0.0	0.2
70.0	$8.00 \cdot 10^{-3}$	0.815	1.6	1.4	0.5	1.1	0.2	0.0	-0.4	0.2	0.1	-0.1	-0.2	0.0	-0.3
70.0	$1.30 \cdot 10^{-2}$	0.708	1.9	1.7	0.5	1.1	0.3	0.0	-0.6	0.8	-0.3	-0.1	0.2	0.0	-0.4
70.0	$2.10 \cdot 10^{-2}$	0.620	1.8	1.6	0.7	1.1	0.4	0.0	-0.6	0.6	-0.2	0.1	0.0	0.0	0.5
70.0	$3.20 \cdot 10^{-2}$	0.557	2.1	2.8	0.9	1.0	0.3	0.0	-0.3	-0.2	0.3	-0.1	-0.2	0.0	2.3
70.0	$5.00 \cdot 10^{-2}$	0.500	1.6	6.2	0.9	1.0	0.3	0.0	-0.7	0.5	-0.2	0.2	-0.1	0.0	6.0
90.0	$2.10 \cdot 10^{-3}$	1.236	2.0	2.2	0.4	1.8	0.2	-0.4	-0.8	0.0	0.4	-0.2	0.2	0.5	0.0
90.0	$3.20 \cdot 10^{-3}$	1.168	1.9	1.7	0.2	1.5	0.4	-0.3	0.3	0.1	0.4	-0.2	-0.1	0.0	0.1
90.0	$5.00 \cdot 10^{-3}$	1.029	1.7	1.7	0.6	1.3	0.2	-0.1	-0.7	-0.1	0.1	-0.2	-0.3	0.0	-0.3
90.0	$8.00 \cdot 10^{-3}$	0.896	1.8	1.5	0.2	1.2	0.7	0.0	-0.4	-0.2	-0.1	-0.2	0.0	0.0	0.1
90.0	$1.30 \cdot 10^{-2}$	0.749	2.1	1.6	1.0	1.1	0.4	0.0	-0.2	0.3	-0.3	-0.1	0.2	0.0	0.1
90.0	$2.10 \cdot 10^{-2}$	0.622	1.9	1.9	0.6	1.1	0.4	0.0	-0.3	0.9	-0.3	0.2	0.1	0.0	-1.0
90.0	$3.20 \cdot 10^{-2}$	0.535	2.3	2.9	1.2	1.0	0.6	0.0	-0.3	0.5	0.2	0.0	-0.1	0.0	2.2
90.0	$5.00 \cdot 10^{-2}$	0.484	2.1	6.3	0.9	1.0	0.2	0.0	0.2	0.1	0.2	0.1	-0.2	0.0	6.1
90.0	$8.00 \cdot 10^{-2}$	0.435	2.0	2.8	0.9	1.0	0.2	0.0	-0.6	0.7	-0.1	0.1	0.0	0.0	2.3
90.0	$1.80 \cdot 10^{-1}$	0.340	3.1	5.3	3.0	1.0	0.7	0.0	-3.1	1.6	-1.4	-0.7	0.0	0.0	-1.8
120.0	$2.10 \cdot 10^{-3}$	1.317	2.2	2.5	0.8	2.0	0.0	0.6	-0.9	0.1	0.1	0.3	-0.6	0.0	-0.1
120.0	$3.20 \cdot 10^{-3}$	1.173	1.9	2.0	0.7	1.7	0.3	0.1	-0.7	0.0	0.3	-0.4	0.0	0.1	0.0
120.0	$5.00 \cdot 10^{-3}$	1.038	1.7	1.8	0.5	1.4	0.5	-0.7	0.1	-0.2	0.4	-0.2	-0.2	0.1	0.0
120.0	$8.00 \cdot 10^{-3}$	0.908	1.8	1.4	0.4	1.2	0.4	-0.3	-0.1	0.1	0.0	-0.1	-0.1	0.0	0.0
120.0	$1.30 \cdot 10^{-2}$	0.760	2.0	1.8	0.5	1.1	0.3	0.0	-1.1	0.2	-0.2	-0.1	-0.1	0.0	0.4
120.0	$2.10 \cdot 10^{-2}$	0.664	1.9	1.8	0.7	1.1	0.4	-0.1	-0.2	1.0	-0.4	0.1	-0.2	0.0	-0.2
120.0	$3.20 \cdot 10^{-2}$	0.579	2.3	2.2	0.9	1.0	0.4	0.0	-0.5	0.1	0.1	0.4	-0.1	0.0	-1.5
120.0	$5.00 \cdot 10^{-2}$	0.472	2.1	5.1	0.8	1.0	0.7	0.0	0.1	-0.3	-0.3	0.1	-0.1	0.0	4.9
120.0	$8.00 \cdot 10^{-2}$	0.437	1.9	4.7	0.7	1.0	0.4	0.0	-0.9	0.6	-0.2	0.0	-0.1	0.0	4.4
120.0	$1.80 \cdot 10^{-1}$	0.328	2.7	8.8	3.2	1.0	0.6	0.0	-2.2	-1.3	-0.9	-0.6	0.0	0.0	-7.6
150.0	$3.20 \cdot 10^{-3}$	1.194	2.1	2.3	0.6	1.9	0.0	0.4	-0.9	-0.1	0.1	0.3	-0.5	0.1	0.0
150.0	$5.00 \cdot 10^{-3}$	1.037	1.9	1.8	0.5	1.5	0.1	0.4	-0.2	0.1	0.5	-0.3	-0.3	0.0	-0.1
150.0	$8.00 \cdot 10^{-3}$	0.887	1.8	1.6	0.7	1.3	0.3	-0.3	-0.4	0.1	-0.2	0.1	-0.2	0.0	0.0

**Table 2** (continued): *Relative uncertainties in the reduced cross section.*

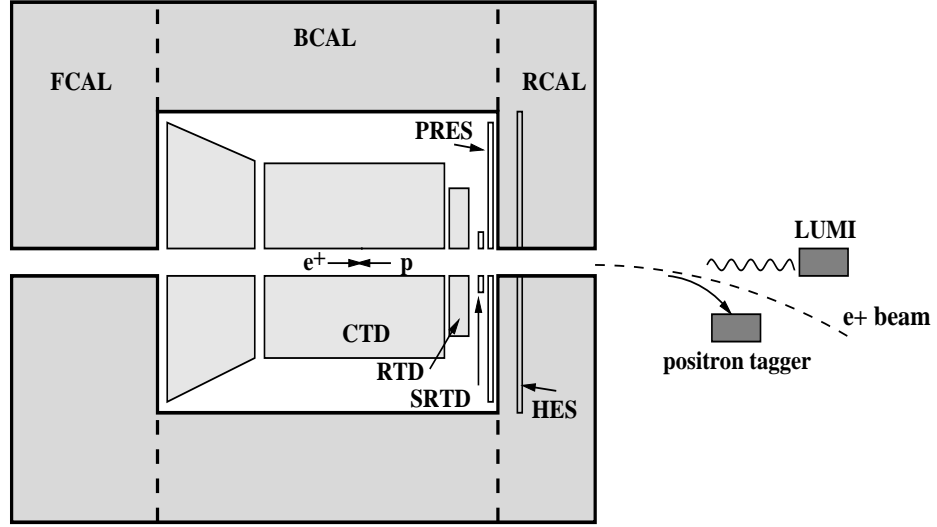
$Q^2$ (GeV <sup>2</sup> )	$x$	$\tilde{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$\delta_{unc}$ (%)	$\delta_{\{1\}}$ (%)	$\delta_{\{2\}}$ (%)	$\delta_{\{3\}}$ (%)	$\delta_{\{4\}}$ (%)	$\delta_{\{5\}}$ (%)	$\delta_{\{6\}}$ (%)	$\delta_{\{7\}}$ (%)	$\delta_{\{8\}}$ (%)	$\delta_{\{9\}}$ (%)	$\delta_{\{10\}}$ (%)
150.0	$1.30 \cdot 10^{-2}$	0.805	2.1	2.0	0.5	1.2	0.4	-1.0	-1.0	0.2	-0.2	-0.1	-0.3	0.0	-0.3
150.0	$2.10 \cdot 10^{-2}$	0.661	2.0	1.9	0.6	1.1	0.5	-0.7	-0.4	0.7	-0.4	0.1	0.0	0.0	0.7
150.0	$3.20 \cdot 10^{-2}$	0.574	2.4	1.7	0.7	1.0	0.3	-0.7	0.0	0.7	-0.2	-0.1	-0.3	0.0	0.3
150.0	$5.00 \cdot 10^{-2}$	0.515	2.2	2.3	1.3	1.0	0.6	-0.5	-0.5	-0.4	0.2	0.2	-0.1	0.0	1.3
150.0	$8.00 \cdot 10^{-2}$	0.431	2.0	5.0	1.0	1.0	0.5	-0.5	-0.4	0.6	0.1	0.1	-0.1	0.0	4.7
150.0	$1.80 \cdot 10^{-1}$	0.326	2.7	6.4	2.3	1.0	0.5	-0.5	-2.5	-1.3	-1.0	-0.4	0.0	0.0	-5.0
200.0	$3.20 \cdot 10^{-3}$	1.162	3.8	3.2	2.0	2.0	0.0	0.8	-1.2	0.2	0.3	0.4	-0.4	0.1	0.0
200.0	$5.00 \cdot 10^{-3}$	1.065	2.3	2.1	0.4	1.7	0.0	0.6	-0.8	-0.1	0.4	-0.3	0.0	0.0	0.2
200.0	$8.00 \cdot 10^{-3}$	0.899	2.2	1.8	0.6	1.4	0.1	0.5	0.6	0.1	0.4	-0.2	0.1	0.0	0.0
200.0	$1.30 \cdot 10^{-2}$	0.794	2.2	1.5	0.2	1.2	0.1	0.3	-0.5	0.2	-0.5	0.0	-0.1	0.0	-0.2
200.0	$2.10 \cdot 10^{-2}$	0.659	2.7	1.8	0.7	1.1	-0.1	0.7	0.5	0.4	-0.7	-0.1	-0.1	0.0	0.1
200.0	$3.20 \cdot 10^{-2}$	0.570	2.8	1.9	0.5	1.1	0.0	0.3	-0.8	0.7	-0.5	0.2	0.0	0.0	0.9
200.0	$5.00 \cdot 10^{-2}$	0.508	2.8	2.4	0.5	1.0	0.3	-0.3	-0.6	-0.4	-0.2	-0.2	-0.1	0.0	2.0
200.0	$8.00 \cdot 10^{-2}$	0.434	2.4	2.7	0.5	1.0	-0.3	-0.7	0.1	0.4	0.4	0.3	-0.1	0.0	2.3
200.0	$1.80 \cdot 10^{-1}$	0.340	2.9	3.7	0.6	1.0	0.3	-0.1	-2.4	-1.2	-0.9	-0.3	0.0	0.0	-1.9
250.0	$5.00 \cdot 10^{-3}$	1.066	3.0	2.9	1.3	1.9	0.0	0.6	-1.6	0.1	0.4	-0.2	0.1	0.0	0.0
250.0	$8.00 \cdot 10^{-3}$	0.927	2.6	1.7	0.5	1.5	0.0	0.5	-0.2	-0.1	0.4	-0.2	-0.1	0.0	0.0
250.0	$1.30 \cdot 10^{-2}$	0.821	2.7	1.8	0.9	1.3	0.0	0.4	0.5	0.3	0.5	0.1	-0.1	0.0	0.4
250.0	$2.10 \cdot 10^{-2}$	0.644	3.5	1.8	0.6	1.1	0.0	-0.4	-0.8	-0.3	-0.3	-0.2	0.0	0.0	-0.7
250.0	$3.20 \cdot 10^{-2}$	0.612	3.4	2.3	1.0	1.1	0.1	0.9	-0.7	0.9	-1.0	0.0	0.1	0.0	-0.3
250.0	$5.00 \cdot 10^{-2}$	0.517	3.2	1.8	1.1	1.0	0.1	0.5	0.3	0.4	-0.1	0.1	-0.2	0.0	-0.3
250.0	$8.00 \cdot 10^{-2}$	0.445	2.8	5.1	0.3	1.0	0.1	1.0	-0.6	-0.2	0.2	-0.3	-0.1	0.0	4.8
250.0	$1.80 \cdot 10^{-1}$	0.341	3.2	5.6	1.1	1.0	0.1	0.5	-1.0	1.3	-0.2	0.3	0.0	0.0	-5.1
350.0	$5.00 \cdot 10^{-3}$	1.103	4.4	3.5	2.7	2.0	0.0	-0.2	-0.6	-0.2	0.3	0.4	0.0	0.0	-0.2
350.0	$8.00 \cdot 10^{-3}$	0.988	2.9	2.1	0.4	1.7	0.0	0.2	-0.8	-0.1	0.8	0.1	-0.4	0.0	-0.2
350.0	$1.30 \cdot 10^{-2}$	0.824	2.9	1.7	0.5	1.3	0.0	0.7	-0.3	-0.1	0.1	-0.1	-0.3	0.0	0.0
350.0	$2.10 \cdot 10^{-2}$	0.679	3.6	1.9	1.1	1.2	0.0	0.8	-0.4	0.2	-0.4	-0.1	0.0	0.0	0.0
350.0	$3.20 \cdot 10^{-2}$	0.639	3.6	2.0	0.8	1.1	0.0	0.6	0.5	0.8	-0.8	0.1	-0.2	0.0	-0.5
350.0	$5.00 \cdot 10^{-2}$	0.526	3.4	1.9	0.6	1.0	0.0	0.8	-0.8	0.3	-0.5	-0.1	-0.1	0.0	0.8
350.0	$8.00 \cdot 10^{-2}$	0.442	3.2	2.6	0.6	1.0	0.0	0.5	-0.7	-0.5	-0.2	0.0	-0.1	0.0	2.1
350.0	$1.80 \cdot 10^{-1}$	0.328	3.5	1.6	0.4	1.0	0.0	0.2	-0.8	0.6	-0.3	0.3	0.0	0.0	-0.3
450.0	$8.00 \cdot 10^{-3}$	0.954	3.5	2.4	1.4	1.8	0.0	-0.2	-0.1	-0.1	0.6	-0.1	-0.1	0.3	-0.1
450.0	$1.30 \cdot 10^{-2}$	0.854	3.0	1.7	0.6	1.4	0.0	0.4	-0.4	0.1	0.3	-0.1	-0.1	0.0	0.1
450.0	$2.10 \cdot 10^{-2}$	0.702	3.6	1.6	0.8	1.2	0.0	0.2	0.5	0.1	0.2	0.1	0.1	0.0	0.2
450.0	$3.20 \cdot 10^{-2}$	0.579	4.3	1.8	0.3	1.1	0.0	0.7	-0.7	0.7	-0.6	-0.1	0.0	0.0	-0.5
450.0	$5.00 \cdot 10^{-2}$	0.511	3.4	1.5	0.5	1.0	0.0	0.3	-0.4	0.6	-0.5	0.1	-0.3	0.0	0.0
450.0	$8.00 \cdot 10^{-2}$	0.439	3.6	2.3	1.1	1.0	0.0	0.5	-0.5	-0.7	-0.1	0.0	-0.1	0.0	1.3
450.0	$1.30 \cdot 10^{-1}$	0.365	3.8	2.3	1.0	1.0	0.0	0.9	-0.2	0.2	0.2	0.1	0.0	0.0	1.6
450.0	$2.50 \cdot 10^{-1}$	0.264	4.5	7.7	1.7	1.0	0.0	0.9	-2.4	-0.8	-0.7	-0.3	0.0	0.0	-6.9
650.0	$8.00 \cdot 10^{-3}$	0.926	4.6	3.2	1.8	1.9	0.0	0.2	-1.5	-0.1	0.0	0.5	-0.7	0.0	0.0
650.0	$1.30 \cdot 10^{-2}$	0.827	3.3	1.9	0.7	1.5	0.0	0.4	-0.3	-0.1	0.6	-0.2	-0.2	0.1	0.1
650.0	$2.10 \cdot 10^{-2}$	0.722	3.8	1.7	0.9	1.2	0.0	0.4	-0.5	0.2	0.3	0.0	0.1	0.0	-0.1
650.0	$3.20 \cdot 10^{-2}$	0.603	4.0	1.9	0.9	1.1	0.0	0.3	-0.4	0.2	-0.1	0.1	0.1	0.0	1.1
650.0	$5.00 \cdot 10^{-2}$	0.475	4.3	2.1	1.0	1.0	0.0	0.4	-0.4	1.1	-0.9	-0.1	0.0	0.0	-0.2
650.0	$8.00 \cdot 10^{-2}$	0.456	3.9	1.5	0.8	1.0	0.0	-0.3	-0.4	-0.3	0.1	0.2	-0.1	0.0	0.6
650.0	$1.30 \cdot 10^{-1}$	0.357	4.2	3.2	1.4	1.0	0.0	0.3	-0.8	0.3	0.2	0.1	0.0	0.0	2.5
650.0	$2.50 \cdot 10^{-1}$	0.250	4.8	3.4	1.7	1.0	0.0	0.7	-1.8	-0.4	-0.6	-0.1	0.0	0.0	1.8
650.0	$4.00 \cdot 10^{-1}$	0.152	9.5	14.5	0.8	1.0	0.0	1.1	-5.6	-3.9	-1.3	-1.3	0.0	0.0	-12.5

**Table 2** (continued): *Relative uncertainties in the reduced cross section.*

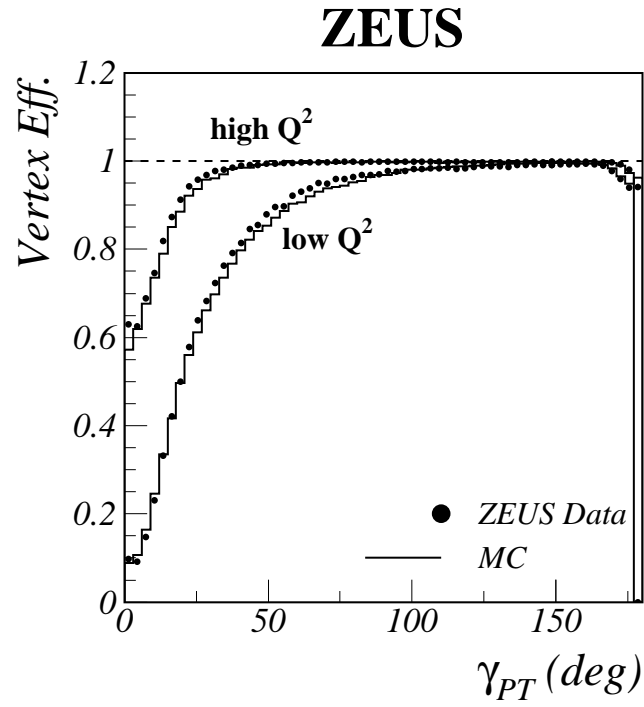
$Q^2$ (GeV <sup>2</sup> )	$x$	$\bar{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$\delta_{unc}$ (%)	$\delta_{\{1\}}$ (%)	$\delta_{\{2\}}$ (%)	$\delta_{\{3\}}$ (%)	$\delta_{\{4\}}$ (%)	$\delta_{\{5\}}$ (%)	$\delta_{\{6\}}$ (%)	$\delta_{\{7\}}$ (%)	$\delta_{\{8\}}$ (%)	$\delta_{\{9\}}$ (%)	$\delta_{\{10\}}$ (%)
800.0	$1.30 \cdot 10^{-2}$	0.847	4.5	2.4	1.0	1.7	0.0	0.3	-1.0	0.0	0.4	-0.2	-0.4	0.0	-0.4
800.0	$2.10 \cdot 10^{-2}$	0.665	7.5	1.6	0.6	1.3	0.0	0.1	0.6	-0.1	0.4	-0.2	0.1	0.0	-0.4
800.0	$3.20 \cdot 10^{-2}$	0.647	4.9	1.4	0.6	1.1	0.0	0.5	-0.4	-0.1	-0.3	0.0	-0.1	0.0	-0.2
800.0	$5.00 \cdot 10^{-2}$	0.451	5.0	2.3	1.3	1.0	0.0	0.3	0.3	1.1	-0.8	0.0	0.0	0.0	0.6
800.0	$8.00 \cdot 10^{-2}$	0.420	5.8	2.6	1.0	1.0	0.0	0.9	-1.4	0.6	-0.4	-0.1	0.0	0.0	1.2
800.0	$1.30 \cdot 10^{-1}$	0.370	5.2	2.5	0.8	1.0	0.0	0.6	-0.7	-0.5	0.0	-0.1	0.0	0.0	-1.9
800.0	$2.50 \cdot 10^{-1}$	0.260	5.9	1.8	0.4	1.0	0.0	-0.1	-0.5	0.3	-0.2	0.2	0.0	0.0	1.3
800.0	$4.00 \cdot 10^{-1}$	0.114	11.4	13.5	2.2	1.0	0.0	0.8	-5.3	-3.1	-0.8	-0.8	0.0	0.0	-11.7
1200.0	$1.40 \cdot 10^{-2}$	0.872	5.5	2.9	1.1	1.7	0.0	0.2	-2.0	0.1	0.5	0.3	-0.3	0.0	0.0
1200.0	$2.10 \cdot 10^{-2}$	0.681	5.1	1.8	0.8	1.3	0.0	0.2	-0.6	-0.1	0.5	-0.1	0.3	0.0	0.0
1200.0	$3.20 \cdot 10^{-2}$	0.563	5.0	2.0	1.5	1.1	0.0	0.3	0.5	0.2	0.1	0.1	0.2	0.0	-0.1
1200.0	$5.00 \cdot 10^{-2}$	0.490	4.6	1.6	1.0	1.0	0.0	0.4	-0.2	0.4	-0.2	-0.2	-0.1	0.0	-0.2
1200.0	$8.00 \cdot 10^{-2}$	0.434	5.3	1.5	0.4	1.0	0.0	-0.1	-0.3	0.7	-0.6	0.2	-0.2	0.0	-0.1
1200.0	$1.30 \cdot 10^{-1}$	0.336	5.8	3.1	0.6	1.0	0.0	0.3	-0.6	0.5	0.1	-0.1	0.0	0.0	2.8
1200.0	$2.50 \cdot 10^{-1}$	0.254	5.4	2.0	1.0	1.0	0.0	0.5	-1.3	-0.3	-0.1	0.1	0.0	0.0	0.1
1200.0	$4.00 \cdot 10^{-1}$	0.149	8.1	10.3	2.9	1.0	0.0	0.3	-3.1	-2.4	-0.7	-0.2	0.0	0.0	-9.0
1200.0	$6.50 \cdot 10^{-1}$	0.021	35.6	25.1	17.5	1.0	0.0	-0.9	-13.3	-5.3	-1.5	-2.2	0.0	0.0	-10.5
1500.0	$2.10 \cdot 10^{-2}$	0.666	7.9	6.2	5.8	1.5	0.0	0.3	1.0	0.0	0.3	-0.4	0.2	0.0	-0.5
1500.0	$3.20 \cdot 10^{-2}$	0.540	10.3	2.0	1.3	1.1	0.0	0.2	-0.2	0.2	0.5	0.0	0.3	0.0	-0.8
1500.0	$5.00 \cdot 10^{-2}$	0.518	5.8	1.8	1.1	1.0	0.0	0.3	-0.4	-0.2	-0.2	-0.1	-0.4	0.0	0.5
1500.0	$8.00 \cdot 10^{-2}$	0.476	5.7	2.6	1.0	1.0	0.0	0.5	-0.6	0.8	-1.0	-0.1	0.1	0.0	-1.6
1500.0	$1.30 \cdot 10^{-1}$	0.301	11.8	1.9	1.2	1.0	0.0	0.2	0.1	-0.1	-0.3	0.2	0.0	0.0	1.0
1500.0	$1.80 \cdot 10^{-1}$	0.313	7.3	5.9	1.2	1.0	0.0	0.2	-0.9	0.6	0.3	-0.1	0.0	0.0	5.6
1500.0	$2.50 \cdot 10^{-1}$	0.270	8.6	3.0	2.2	1.0	0.0	0.1	-1.7	-0.5	-0.1	0.1	0.0	0.0	0.0
1500.0	$4.00 \cdot 10^{-1}$	0.146	12.6	13.7	1.9	1.0	0.0	0.4	-3.9	-1.7	-0.9	-0.2	0.0	0.0	-12.8
1500.0	$6.50 \cdot 10^{-1}$	0.012	30.9	19.0	8.8	1.0	0.0	0.8	-7.6	-6.0	-1.0	-0.4	0.0	0.0	13.6
2000.0	$3.20 \cdot 10^{-2}$	0.586	8.3	3.4	3.1	1.1	0.0	0.4	-0.4	-0.1	0.5	-0.2	-0.4	0.0	0.6
2000.0	$5.00 \cdot 10^{-2}$	0.476	7.4	2.0	1.4	1.0	0.0	0.3	-0.8	0.1	0.0	0.1	-0.2	0.0	-0.4
2000.0	$8.00 \cdot 10^{-2}$	0.444	7.1	2.0	1.1	1.0	0.0	0.3	-0.3	0.8	-0.6	0.1	-0.1	0.0	0.8
2000.0	$1.30 \cdot 10^{-1}$	0.340	8.3	3.9	1.9	1.0	0.0	0.3	-0.6	0.4	-0.4	-0.1	0.0	0.0	-3.1
2000.0	$1.80 \cdot 10^{-1}$	0.282	9.1	2.6	1.8	1.0	0.0	0.4	-1.2	-0.7	0.1	-0.1	0.0	0.0	-0.5
2000.0	$2.50 \cdot 10^{-1}$	0.234	10.4	5.3	2.3	1.0	0.0	0.4	-0.9	-0.4	-0.2	0.1	0.0	0.0	4.5
2000.0	$4.00 \cdot 10^{-1}$	0.170	13.8	10.1	2.0	1.0	0.0	-0.2	-4.0	-2.5	-0.5	-0.2	0.0	0.0	-8.6
3000.0	$5.00 \cdot 10^{-2}$	0.542	8.7	2.1	1.6	1.0	0.0	0.1	0.9	-0.1	0.4	-0.2	0.2	0.0	-0.1
3000.0	$8.00 \cdot 10^{-2}$	0.438	8.5	2.2	0.8	1.0	0.0	0.3	-0.4	-0.1	-0.3	0.0	-0.2	0.0	-1.6
3000.0	$1.30 \cdot 10^{-1}$	0.325	13.9	4.4	1.4	1.0	0.0	0.3	0.6	1.3	-1.0	-0.1	0.0	0.0	3.7
3000.0	$1.80 \cdot 10^{-1}$	0.243	11.7	3.8	1.4	1.0	0.0	0.3	-1.0	-0.5	-0.1	0.1	0.0	0.0	-3.1
3000.0	$2.50 \cdot 10^{-1}$	0.193	17.7	4.2	2.2	1.0	0.0	-0.2	-1.3	-0.5	-0.1	-0.2	0.7	0.0	-3.1
3000.0	$4.00 \cdot 10^{-1}$	0.089	21.7	9.1	6.7	1.0	0.0	0.5	-4.3	-1.3	-0.6	0.4	0.0	0.0	4.1
3000.0	$6.50 \cdot 10^{-1}$	0.016	33.9	15.3	8.1	1.0	0.0	-0.1	-10.8	-7.0	-0.7	-0.2	0.0	0.0	1.1
5000.0	$8.00 \cdot 10^{-2}$	0.376	9.0	2.7	2.2	1.0	0.0	0.2	-0.9	0.0	0.5	0.0	0.1	0.6	0.0
5000.0	$1.30 \cdot 10^{-1}$	0.284	11.7	2.0	0.8	1.0	0.0	0.4	1.3	0.6	-0.6	0.0	0.0	0.0	0.3
5000.0	$1.80 \cdot 10^{-1}$	0.278	11.3	5.2	2.4	1.0	0.0	0.1	-0.7	0.3	-0.5	0.1	0.0	0.0	4.4
5000.0	$2.50 \cdot 10^{-1}$	0.223	13.2	3.5	2.6	1.0	0.0	0.2	-2.1	0.5	0.1	-0.2	0.0	0.0	0.1
5000.0	$4.00 \cdot 10^{-1}$	0.126	18.3	5.4	1.6	1.0	0.0	-0.3	-2.9	-1.6	-0.3	0.3	0.0	0.0	-3.8
8000.0	$1.30 \cdot 10^{-1}$	0.241	14.5	4.2	4.0	1.0	0.0	0.3	-0.7	-0.1	-0.1	0.0	0.0	0.0	0.0
8000.0	$1.80 \cdot 10^{-1}$	0.272	15.4	5.6	3.6	1.0	0.0	0.3	-0.5	1.0	-0.8	-0.1	0.0	0.0	4.0
8000.0	$2.50 \cdot 10^{-1}$	0.199	18.1	10.8	0.6	1.0	0.0	0.5	-1.6	-0.9	-0.1	0.1	0.0	0.0	-10.6

**Table 2** (continued): *Relative uncertainties in the reduced cross section.*

$Q^2$ (GeV <sup>2</sup> )	$x$	$\bar{\sigma}^{e^+p}$	$\delta_{stat}$ (%)	$\delta_{sys}$ (%)	$\delta_{unc}$ (%)	$\delta_{\{1\}}$ (%)	$\delta_{\{2\}}$ (%)	$\delta_{\{3\}}$ (%)	$\delta_{\{4\}}$ (%)	$\delta_{\{5\}}$ (%)	$\delta_{\{6\}}$ (%)	$\delta_{\{7\}}$ (%)	$\delta_{\{8\}}$ (%)	$\delta_{\{9\}}$ (%)	$\delta_{\{10\}}$ (%)
8000.0	$4.00 \cdot 10^{-1}$	0.119	23.8	6.8	0.8	1.0	0.0	-0.2	-4.1	-1.6	-0.4	-0.2	0.0	0.0	5.0
8000.0	$6.50 \cdot 10^{-1}$	0.036	30.6	14.2	5.7	1.0	0.0	-0.6	-8.1	-4.1	-0.2	0.1	0.0	0.0	-9.1
12000.0	$1.80 \cdot 10^{-1}$	0.238	20.1	3.7	3.1	1.0	0.0	0.2	-1.7	0.2	0.3	0.1	0.0	0.0	0.1
12000.0	$2.50 \cdot 10^{-1}$	0.172	25.9	4.1	3.7	1.0	0.0	0.1	-0.6	0.4	-0.3	-0.1	0.0	0.0	1.2
12000.0	$4.00 \cdot 10^{-1}$	0.084	38.0	3.3	0.8	1.0	0.0	0.5	-2.7	-1.2	0.0	-0.1	0.0	0.0	0.5
20000.0	$2.50 \cdot 10^{-1}$	0.161	35.4	5.2	4.8	1.0	0.0	0.7	-1.5	0.0	0.1	0.0	0.0	0.0	-0.1
20000.0	$4.00 \cdot 10^{-1}$	0.080	$^{+79}_{-48}$	13.9	12.6	1.0	0.0	-0.5	-4.7	-1.4	-0.5	-0.1	0.0	0.0	-3.0
30000.0	$4.00 \cdot 10^{-1}$	0.039	$^{+230}_{-83}$	6.8	4.6	1.0	0.0	0.5	-4.9	-0.4	0.2	0.0	0.0	0.0	-0.6

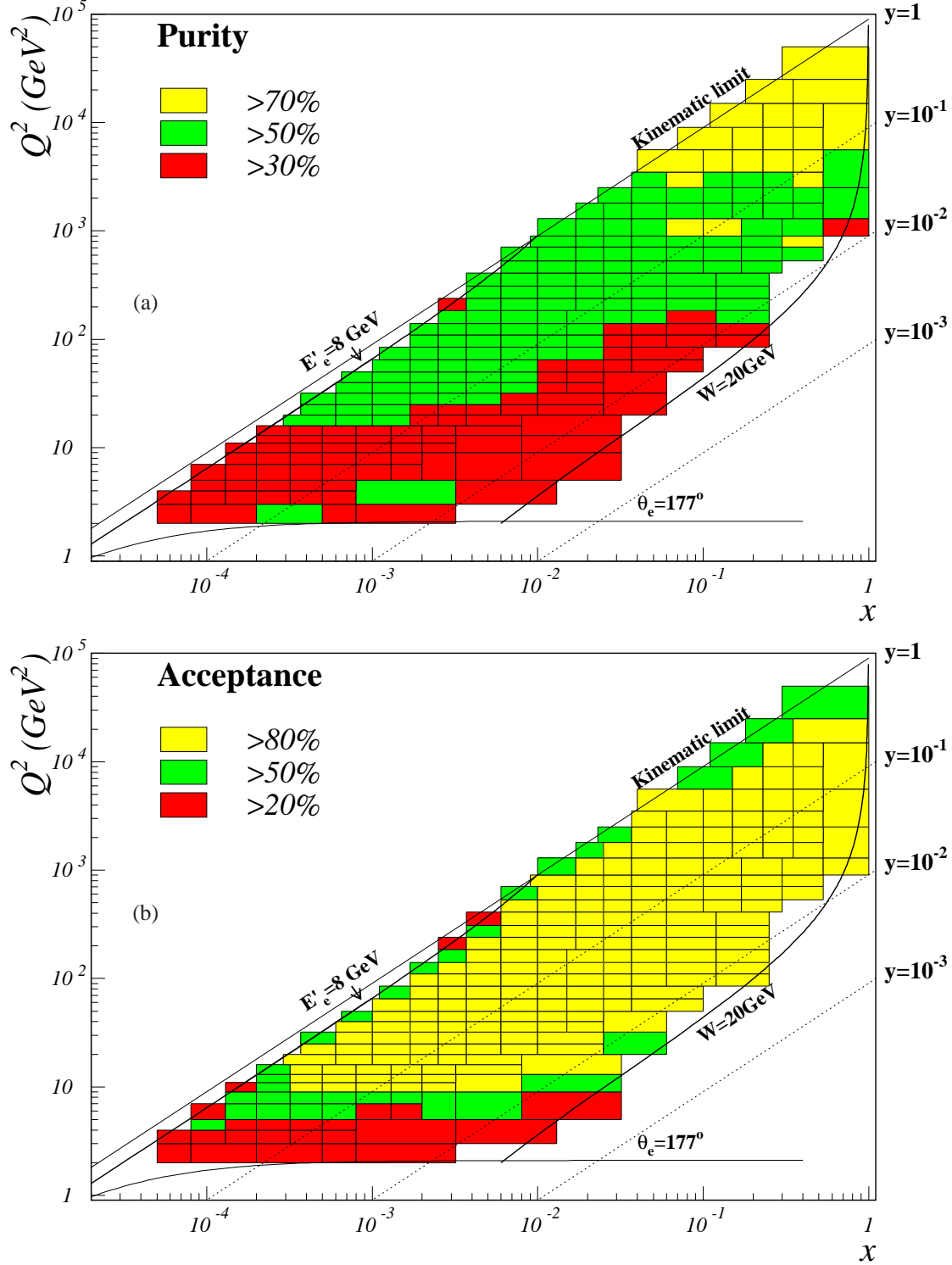


**Figure 1:** Schematic view of the ZEUS detector showing those components important for this analysis.



**Figure 2:** Vertex finding efficiency as a function of the hadronic angle  $\gamma_{PT}$ , defined in Eq. (6).

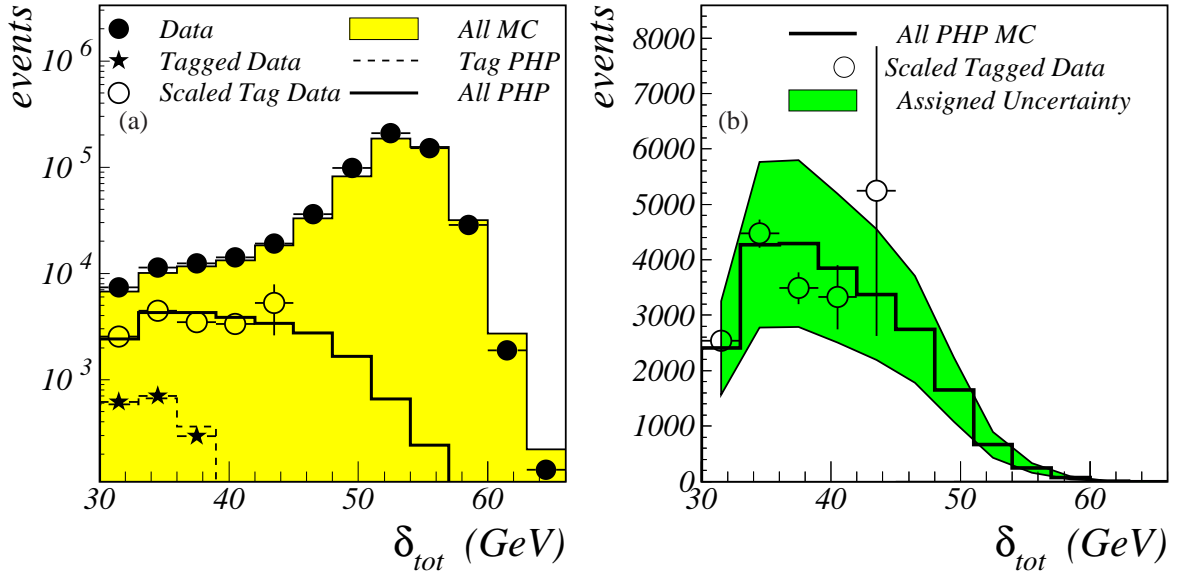
# ZEUS



**Figure 3:** a) The purity. b) The acceptance. The analysis binning is shown, together with the limits of the ZEUS acceptance. At the edges of the kinematic plane, the acceptance is lower due to the various selection criteria. The rear beamhole limits the acceptance of events with small angles of the scattered positron to  $Q^2 \gtrsim 2$  GeV $^2$ . For  $y \gtrsim 0.7$ , the positron energy cut and for  $Q^2 \gtrsim 1000$  GeV $^2$  and  $y = 1$  the kinematic limit of HERA constrains the measurements. The forward beamhole limits the acceptance to  $y \gtrsim 0.004$  for events with small angles of the hadronic system; this limit is shown by the line  $W = 20$  GeV.

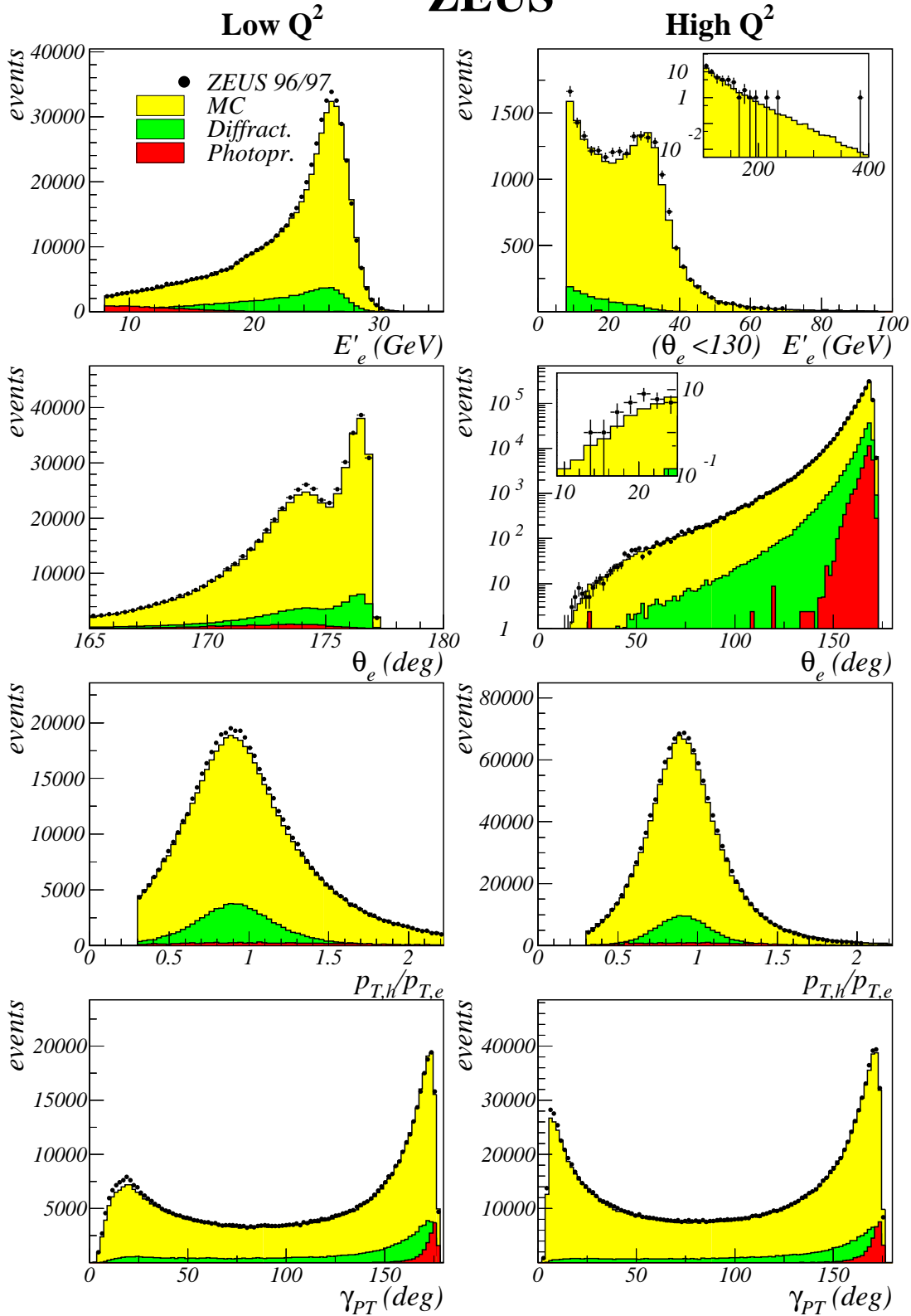


# ZEUS

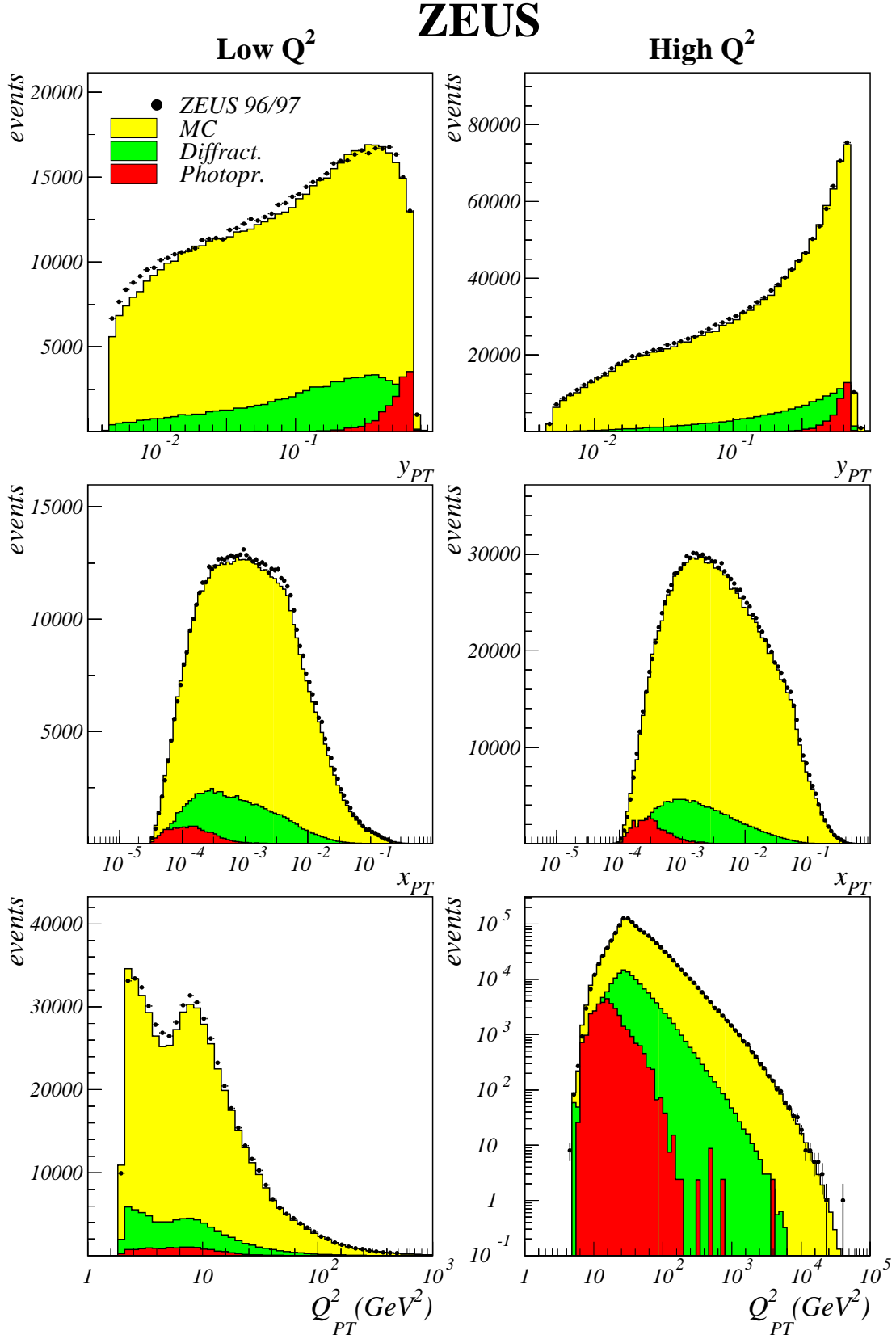


**Figure 4:** a) Distribution of  $\delta$ , see Eq. (3), for the low- $Q^2$  sample (filled circles), for that subset of the data tagged by the positron tagger (stars) and for these tagged data corrected for the acceptance of the positron tagger (open circles). The lines show MC distributions after reweighting as discussed in the text. b) The photoproduction MC (PHP) and the scaled tagged data are shown on a linear scale. The shaded area shows the uncertainty assigned to the photoproduction background, see Section 10.2.

# ZEUS

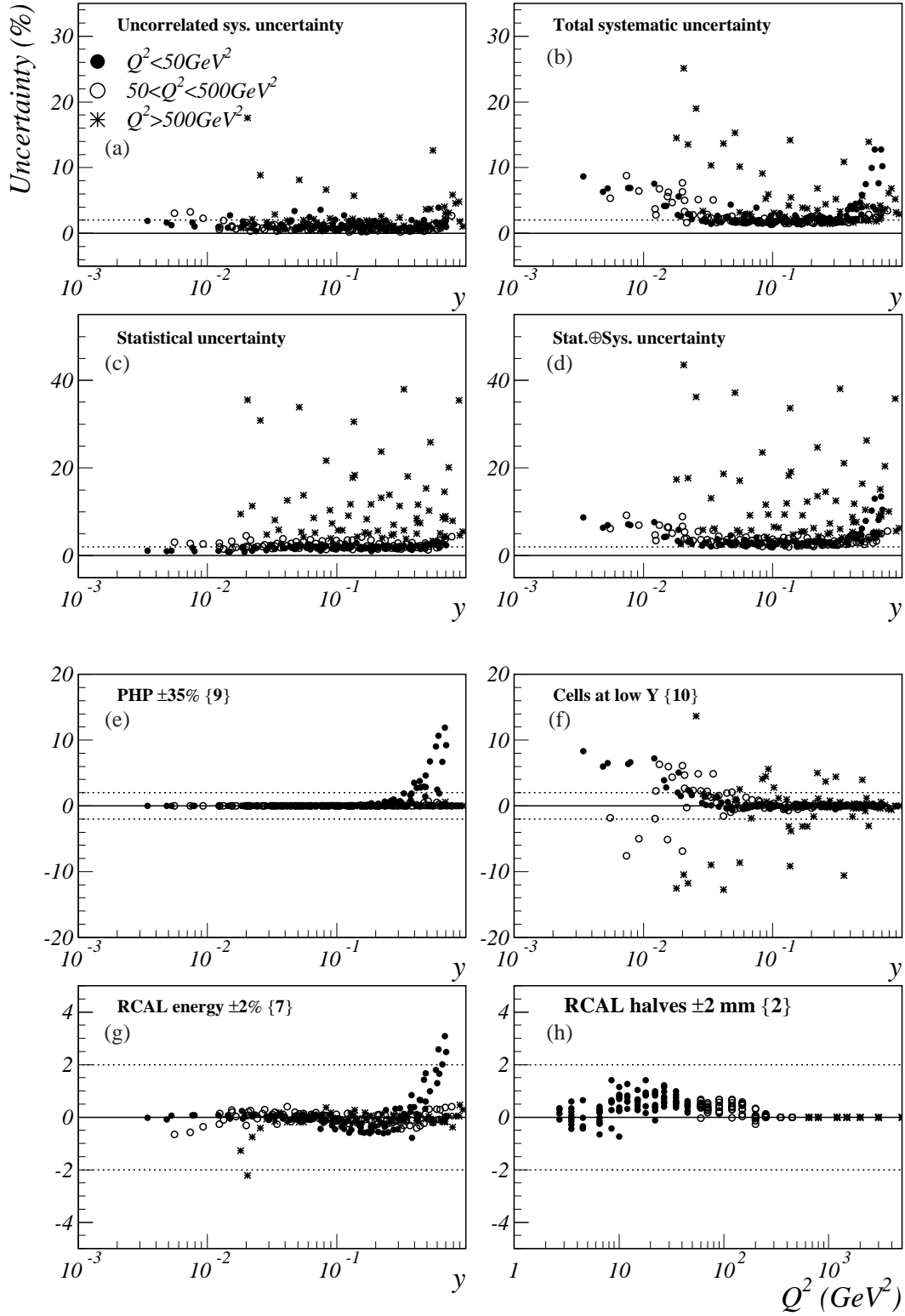


**Figure 5:** Distributions of measured quantities, as discussed in the text, are shown for the low- $Q^2$  sample and the high- $Q^2$  sample. The MC histograms are based on the NLO QCD fit to the data and are normalised according to the luminosity. The diffractive component and the photoproduction background contributions are separately shown. The inserts show details of the corresponding distributions.



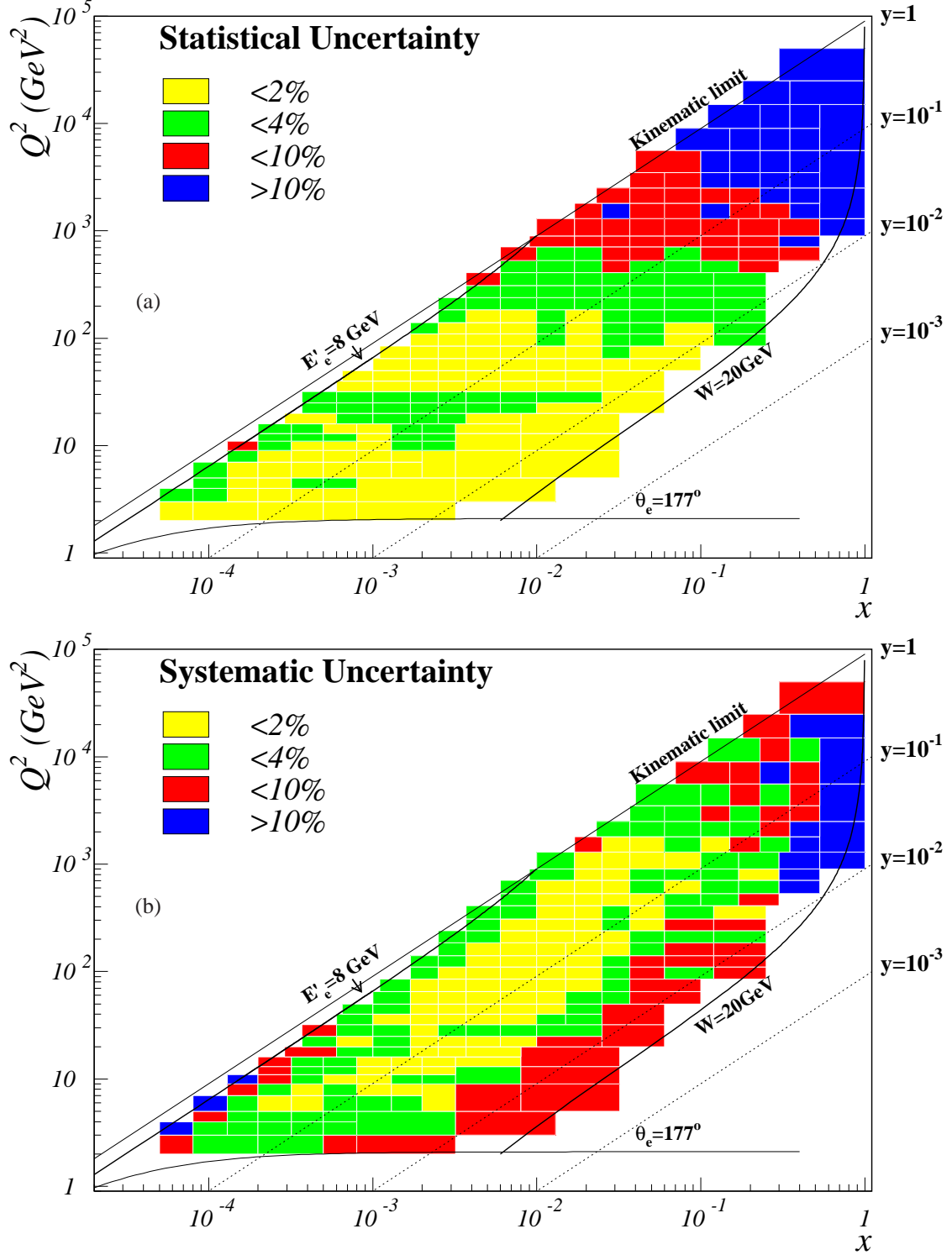
**Figure 6:** Distributions of kinematic variables are shown for the low- $Q^2$  sample and the high- $Q^2$  sample. The MC histograms are based on the NLO QCD fit to the data and are normalised according to the luminosity. The diffractive component and the photoproduction background contributions are separately shown.

# ZEUS



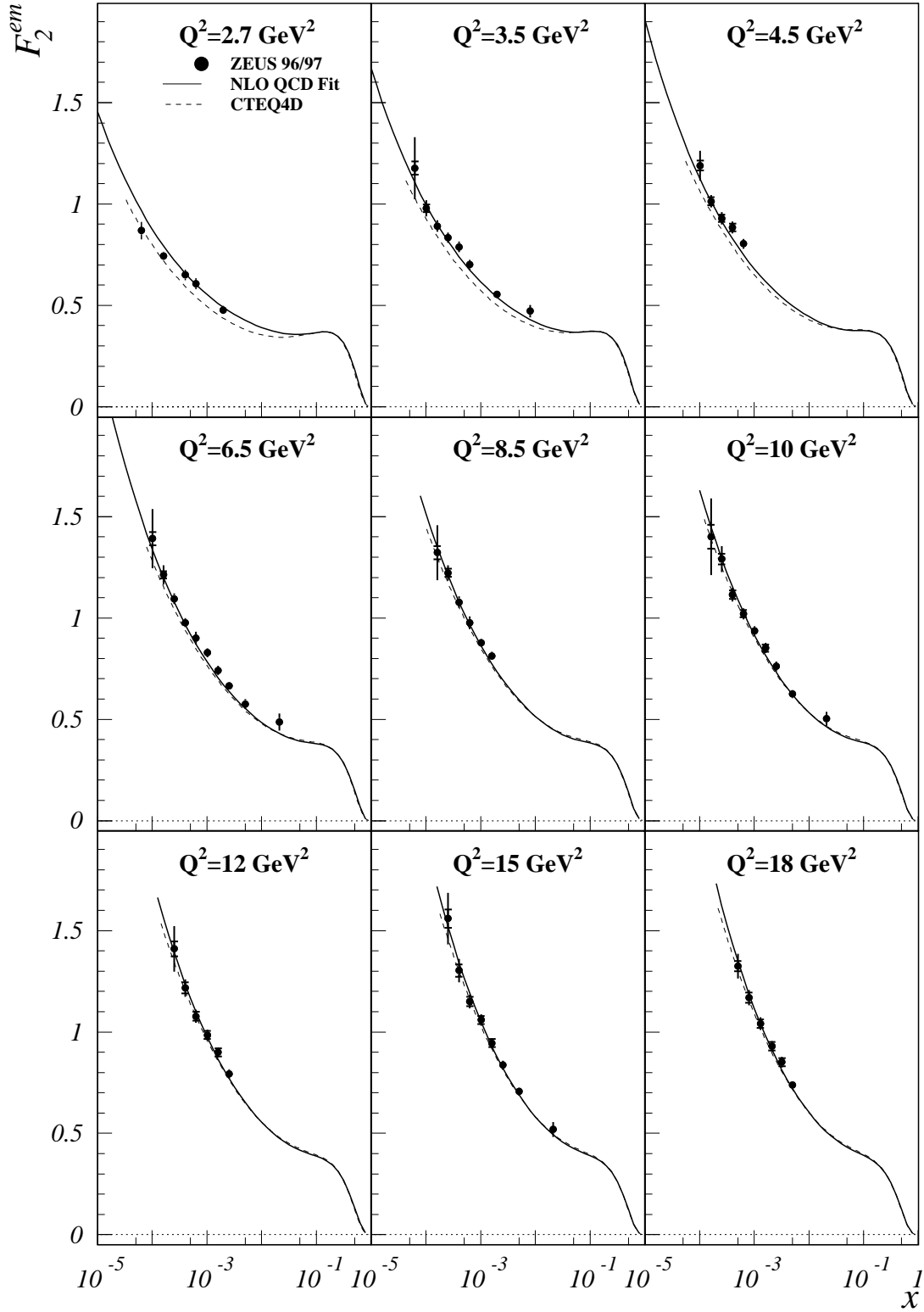
**Figure 7:** (a-d) The relative uncorrelated systematic, total systematic, statistical, and total systematic uncertainty. Three regions in  $Q^2$  are denoted by different symbols. (e-h) Four typical sources of the correlated systematic uncertainty, where the number in  $\{\}$  corresponds to the number in Section 10.2. The dotted lines are at  $\pm 2\%$ .

# ZEUS



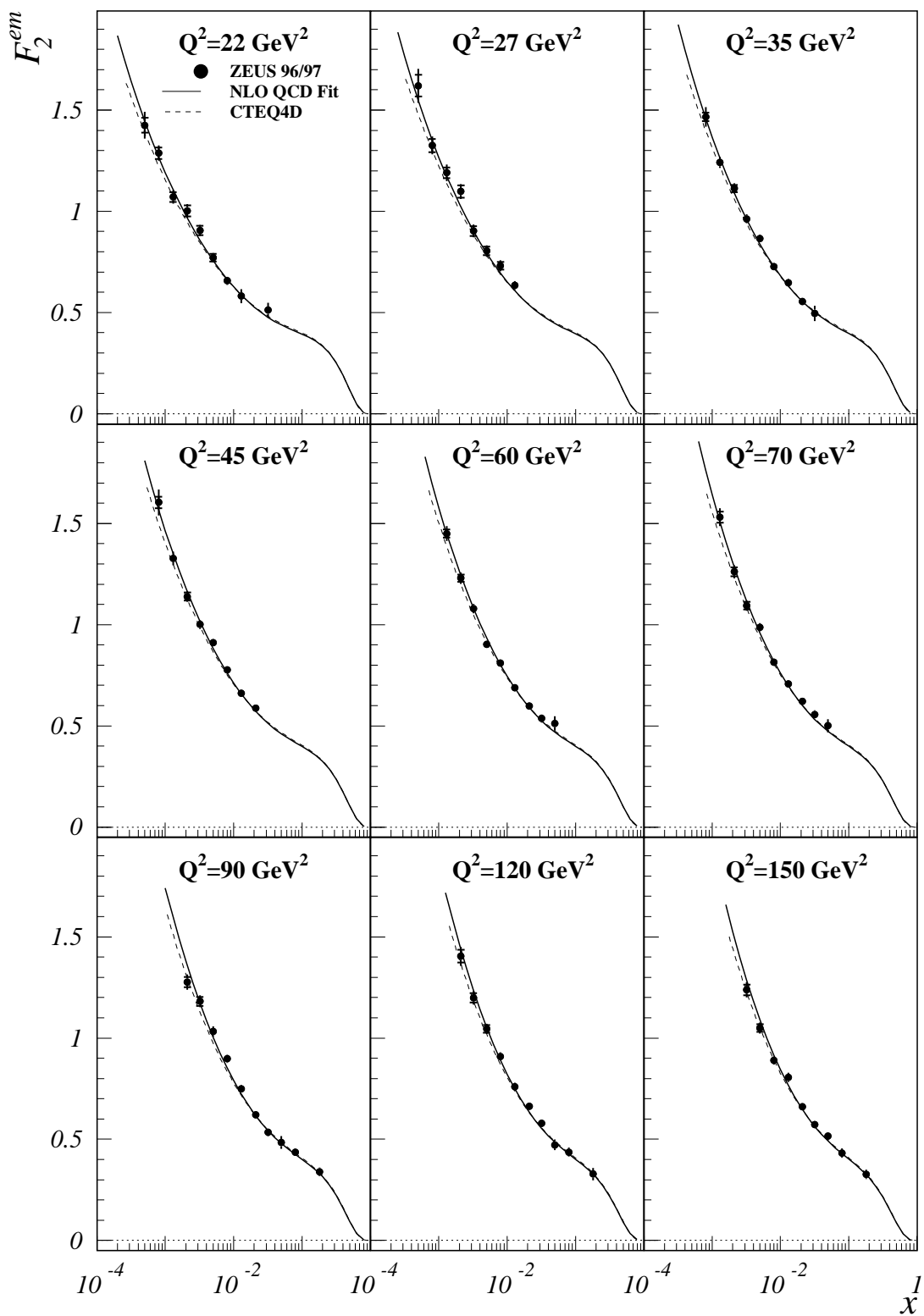
**Figure 8:** a) The statistical uncertainty. b) The systematic uncertainty. Over a large region of phase space both the statistical and systematic uncertainties are below 2%. At the edges of the measurable region the systematic uncertainty increases to  $\sim 10\%$ . For  $y \gtrsim 0.5$  the uncertainty increases due to the uncertainty on the photoproduction background, whereas for  $y \lesssim 0.01$  the uncertainty increases mainly because of uncertainties on the hadronic energy flow.

# ZEUS



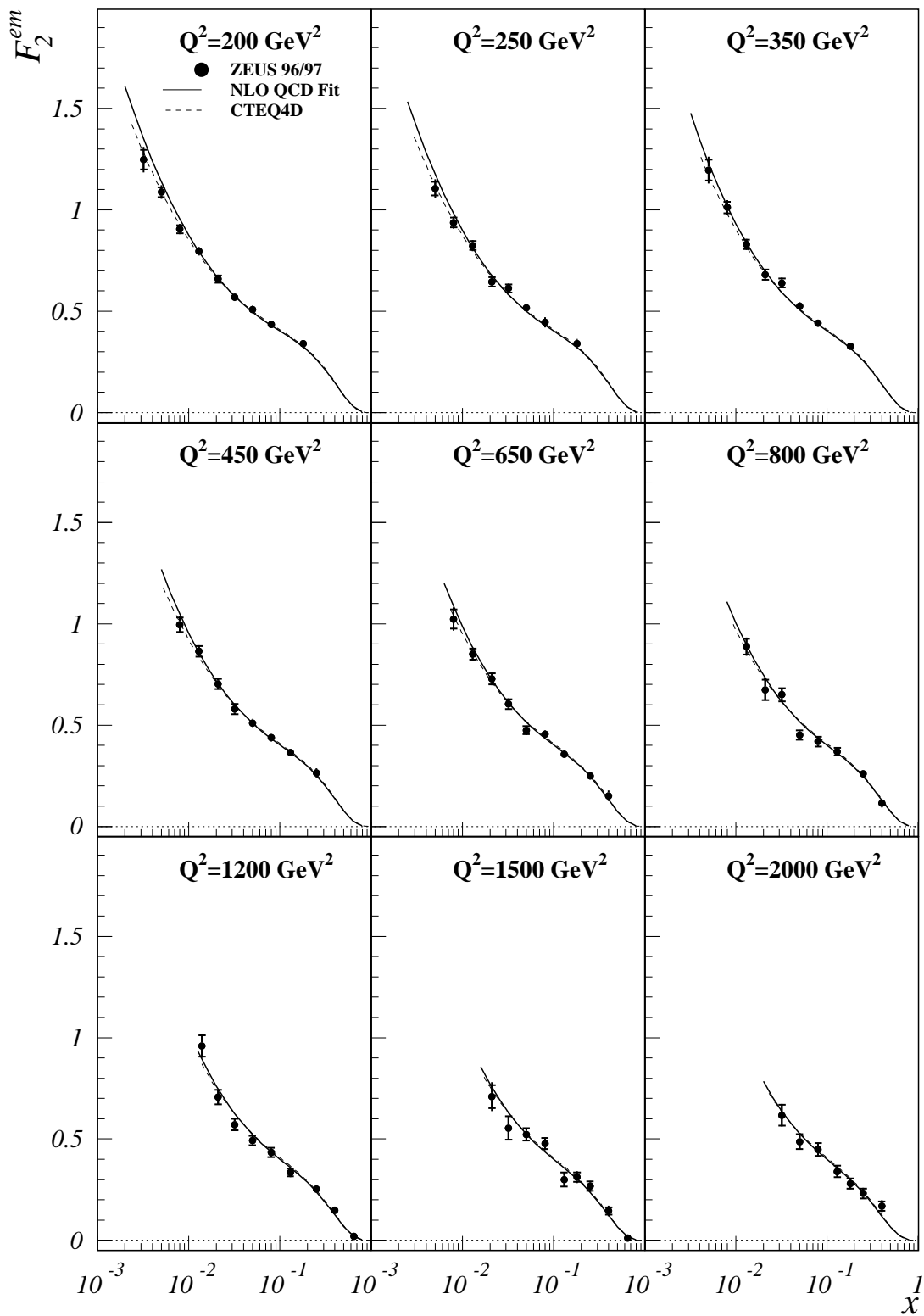
**Figure 9:** The results for  $F_2^{em}$  (points) are shown versus  $x$  for fixed  $Q^2$ . The full curves show results from the ZEUS NLO QCD fit and the dashed curves show predictions from CTEQ4D. The inner error bars (delimited by the horizontal lines) show the statistical uncertainties; the outer ones show the statistical and systematic uncertainties added in quadrature. The overall normalisation uncertainties, see Section 10.2, are not included.

# ZEUS



**Figure 10:** The results for  $F_2^{em}$  (points) are shown versus  $x$  for fixed  $Q^2$ . For details, see caption of Fig. 9.

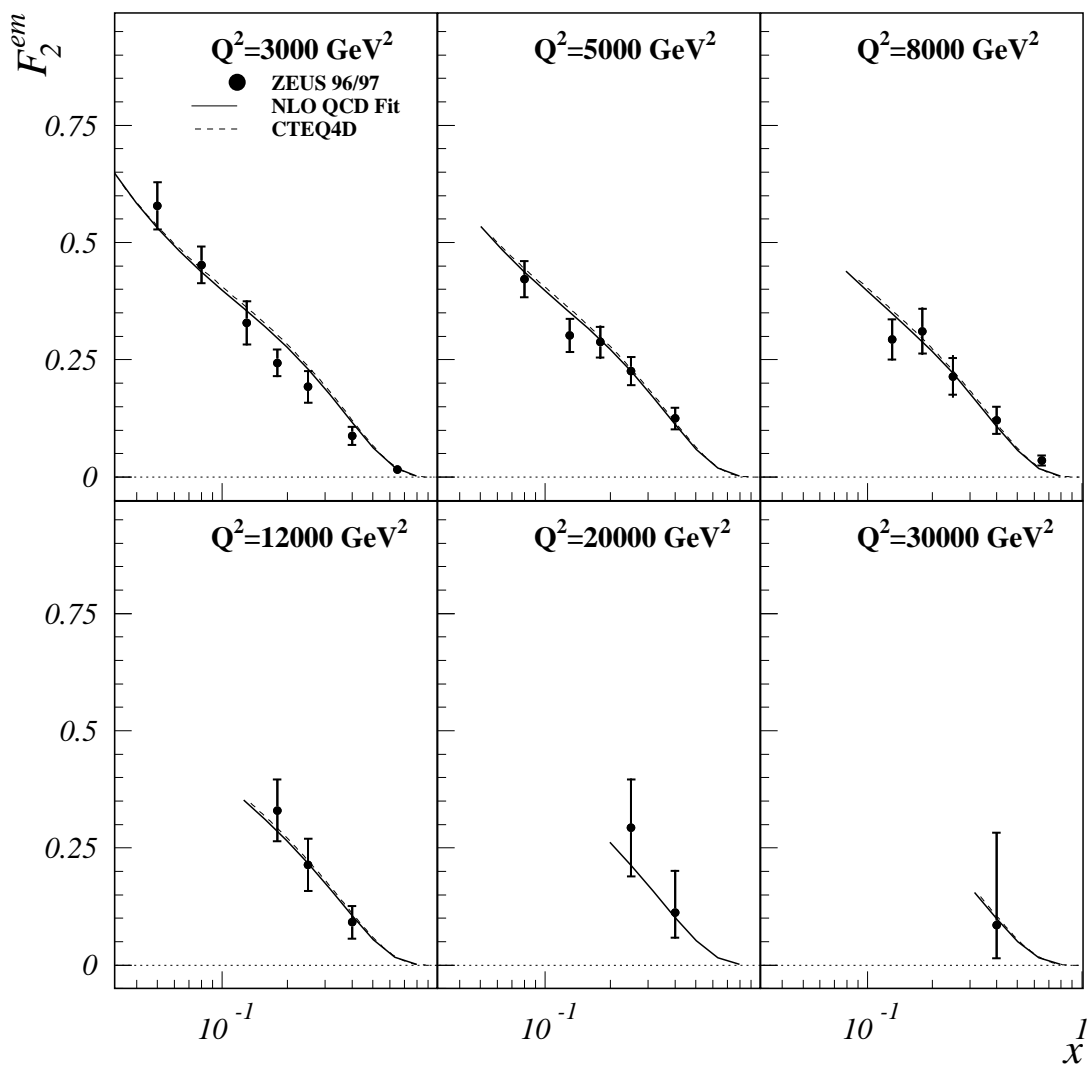
# ZEUS



**Figure 11:** The results for  $F_2^{em}$  (points) are shown versus  $x$  for fixed  $Q^2$ . For details, see caption of Fig. 9.

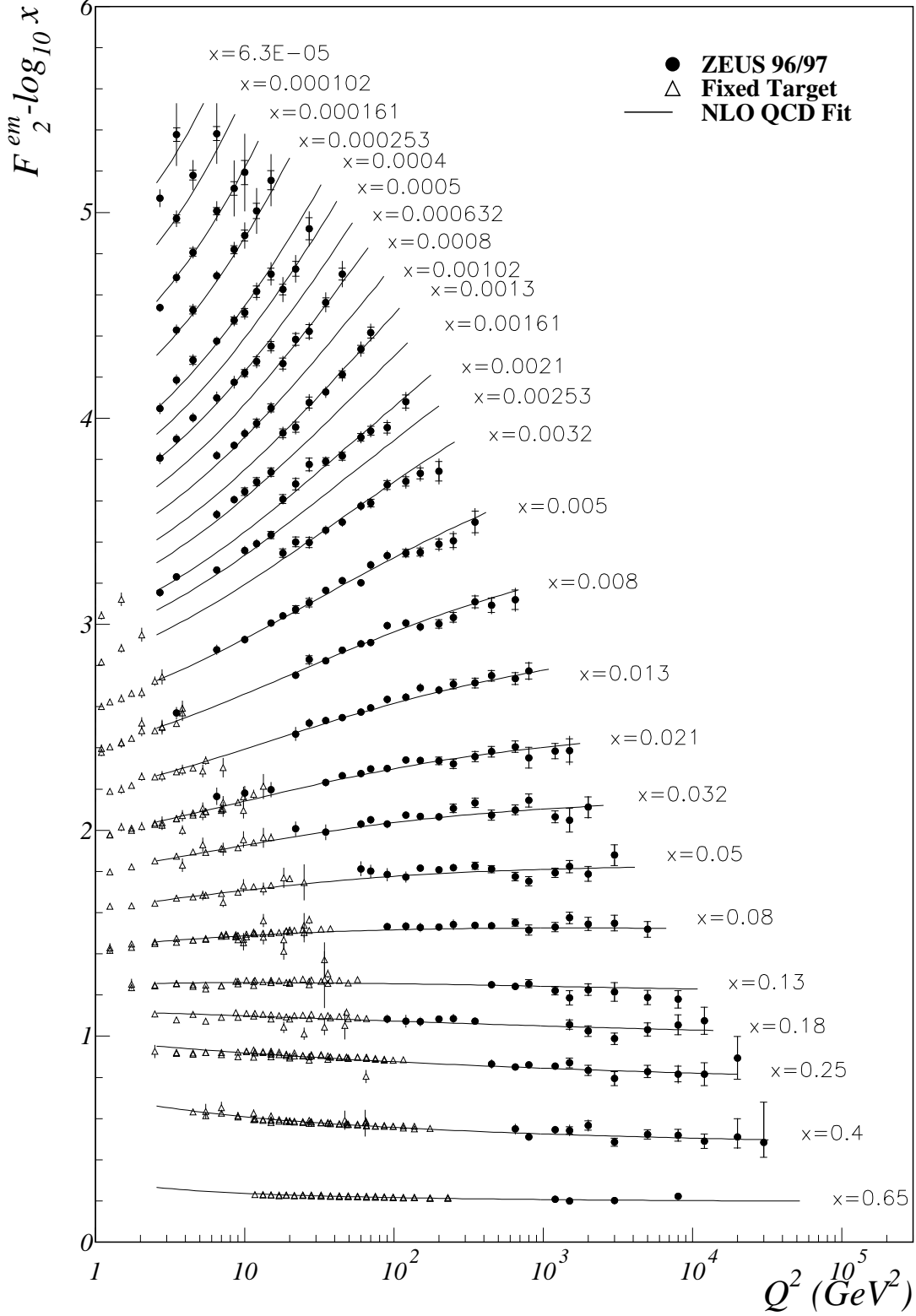


# ZEUS



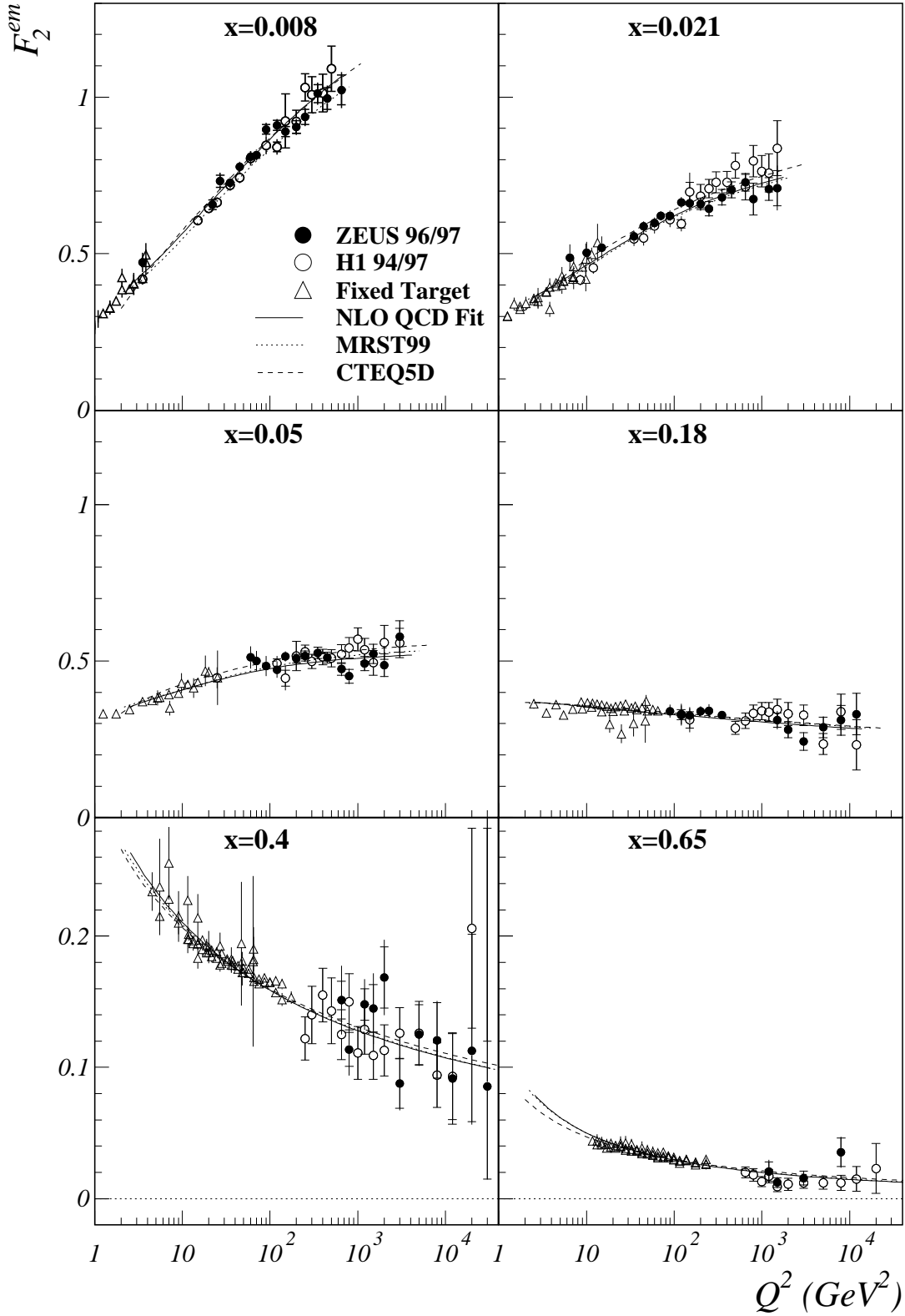
**Figure 12:** The results for  $F_2^{em}$  (points) are shown versus  $x$  for fixed  $Q^2$ . For details, see caption of Fig. 9.

# ZEUS



**Figure 13:** The results for  $F_2^{em}$  (points) versus  $Q^2$  are shown for fixed  $x$ . The fixed target results from NMC, BCDMS and E665 (triangles) and the ZEUS NLO QCD fit (curve) are also shown.

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**Figure 14:** The results for  $F_2^{em}$  versus  $Q^2$ , for six bins at fixed  $x$ , are compared with results from NMC, BCDMS, E665 (triangles) and the recently published H1 results (open symbols). The inner error bars (delimited by the horizontal lines) show the statistical uncertainties; the outer ones show the statistical and systematic uncertainties added in quadrature, both for ZEUS and H1.